

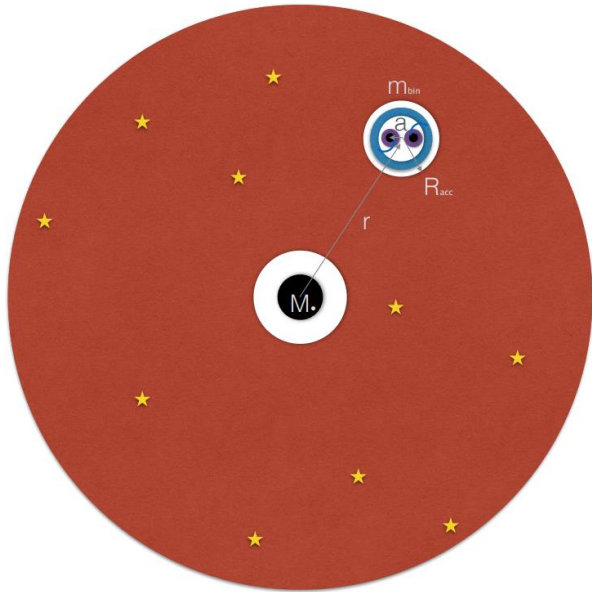
# Long-term Evolution of Tightly-Packed Stellar Black Holes in AGN Disks: Formation of Merging Black-Hole Binaries via Close Encounters

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[arxiv:2203.05584](https://arxiv.org/abs/2203.05584)

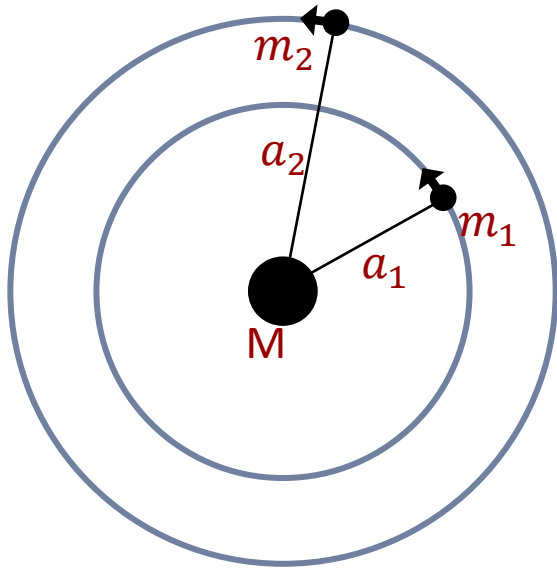
## Why do we care about black hole binaries in AGN disks?



Stone et al. 2017

- Because they may merge! (e.g., Baruteau et al. 2011; Stone et al. 2017; Leigh et al. 2018; Samsing et al. 2020; Li et al. 2021, 2022; Li & Lai 2022)
- **Q: How to form BH binaries in AGN disks? ----- Close encounters between embedded single BHs.**

Our study: long-term **N-body simulations** of SMBH + embedded BHs



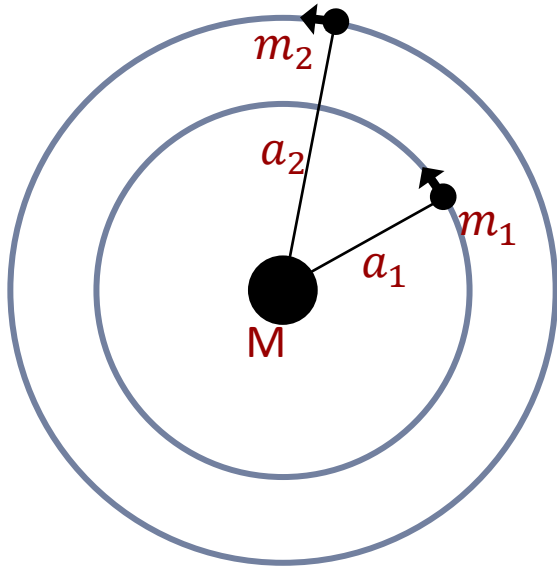
- Initial condition:

$$a_2 - a_1 = 2R_H \quad \text{where} \quad R_H = \frac{a_1 + a_2}{2} \left( \frac{m_1 + m_2}{3M} \right)^{1/3}$$

**(Dynamical instability will occur!)**

- Reasons for using closely-packed orbits:
  - Large BH population in an AGN disk
  - Differential migration

## Our study: long-term **N-body simulations** of SMBH + embedded BHs



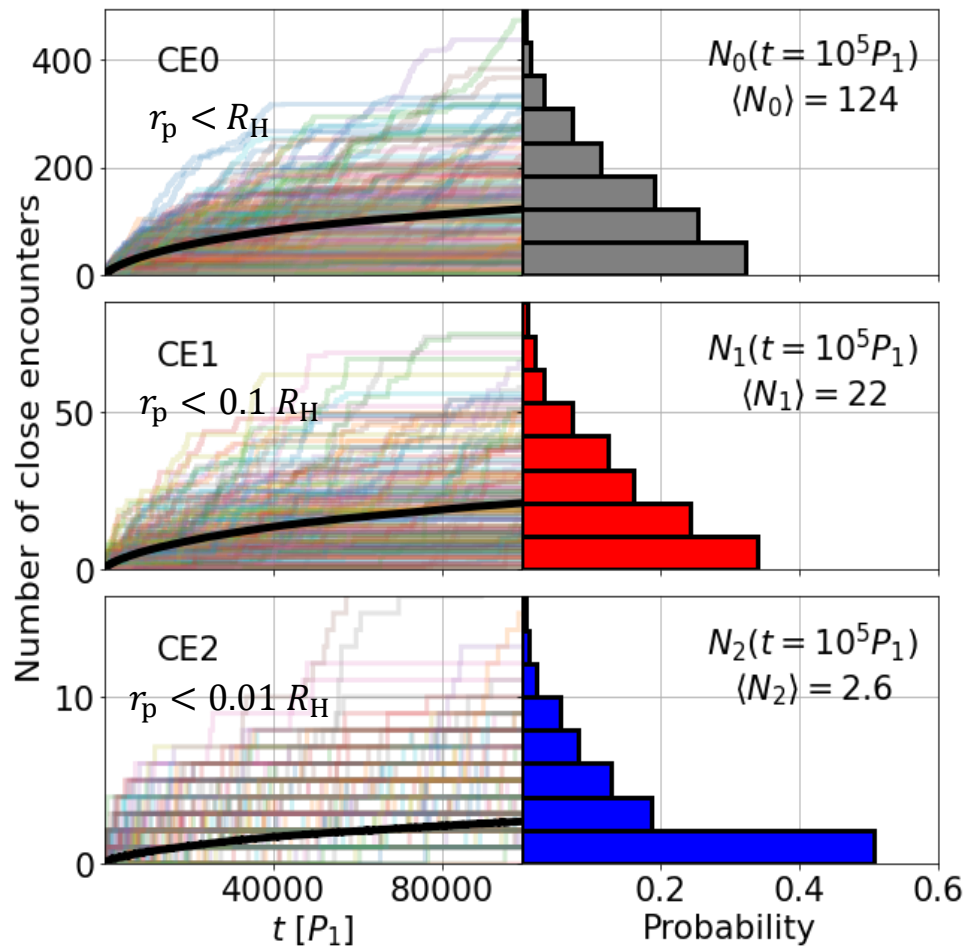
- Simulations:
  - Run for at least  $10^5 P_1$  (orbits around the SMBH)
  - Pure N-body and **no gas effect** for now (gas effect is discussed in the paper).
- Outcomes of this instability:
  - BH collisions? -- unlikely
  - BH ejections? -- requires very long time
  - **Recurring close encounters** -- will be many! (we can study this stochastic process statistically)

## Pure N-body results

### Number of close encounters (CE)

$r_p$ : minimum BH separation during a CE

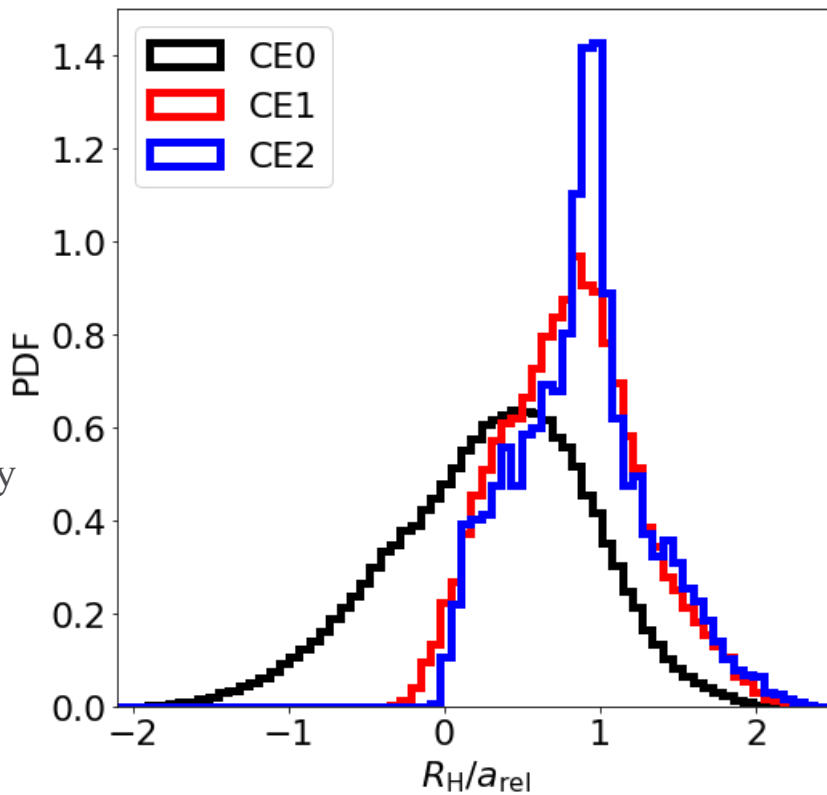
$P_1$ : orbital period around the SMBH



## Pure N-body results

$$R_H/a_{\text{rel}} = \frac{Gm_1m_2}{2a_{\text{rel}}} / \frac{Gm_1m_2}{2R_H}$$

Most BH pairs at close encounters are disrupted by the **SMBH tidal force** within 1  $P_1$ .



## Hardening BH encounters with GW radiation

- BHs can be captured into long-lived binary if enough energy is radiated **at once**:

$$\Delta E_{\text{GW}} = \frac{85\pi}{12\sqrt{2}} \frac{G^{7/2} \mu^2 m_{12}^{5/2}}{c^5 r_p^{7/2}}$$

**energy radiated by GW  
(Quinlan & Shapiro 1989)**

$$\gtrsim \eta \frac{Gm_1m_2}{R_{\text{H}12}}$$

**energy needs to be  
removed for binding**

- $r_p$  needs to be smaller than a critical capture radius:

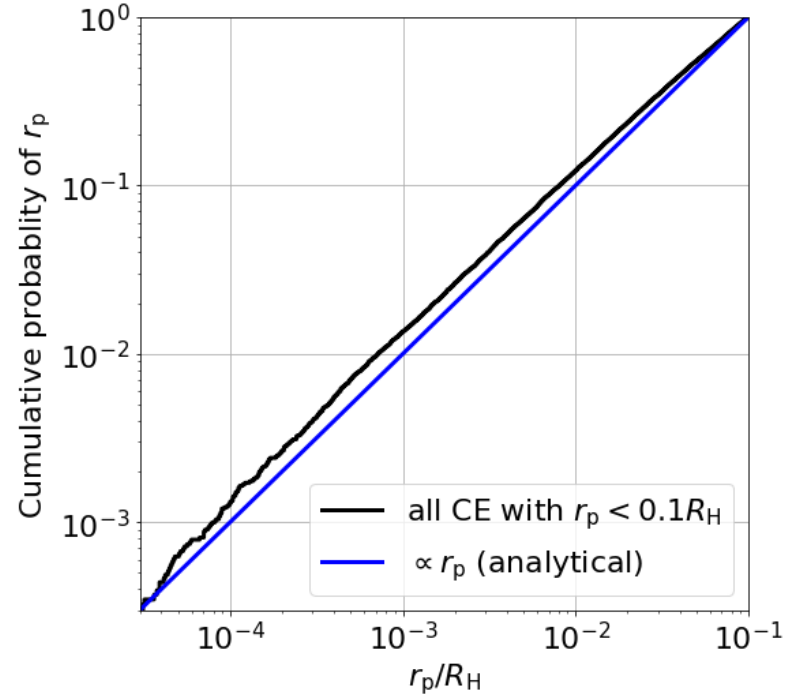
$$\frac{r_p}{R_{\text{H}}} < \frac{r_{\text{cap}}}{R_{\text{H}}} \simeq 10^{-4} \left( \frac{4\mu}{m_{12}} \right)^{\frac{2}{7}} \left( \frac{10^6 m_{12}}{M} \right)^{\frac{10}{21}} \left( \frac{a_{\text{SMBH}}}{100GM/c^2} \right)^{-5/7}$$

## Hardening BH encounters with GW radiation

- $r_p$  needs to be smaller than the critical capture radius:

$$\frac{r_p}{R_H} < \frac{r_{\text{cap}}}{R_H} \simeq 10^{-4}$$

- We show numerically and analytically that  **$r_p$  follows a power-law cumulative probability distribution**, which allows  $r_p$  to be arbitrarily small.





Calculate the GW capture rate:

**Number of binaries formed = (Probability of  $r_p < r_{\text{cap}}$  for one CE)  $\times$  (Number of CEs)**

$$\langle N_{\text{capture}} \rangle \simeq 6 \times 10^{-5} \left( \frac{t}{P_1} \right)^{0.52} \left( \frac{r_{\text{cap}}}{10^{-4} R_H} \right)$$

Fiducial results: Average systems take  $\sim 10^8 P_1$  to get one GW capture.

*\* We expect these captured binaries to merge quickly. Their mergers will show **high eccentricities** when entering the LIGO band.*

# Dissipation through disk gas

- Drag force and torque from the AGN disk:**

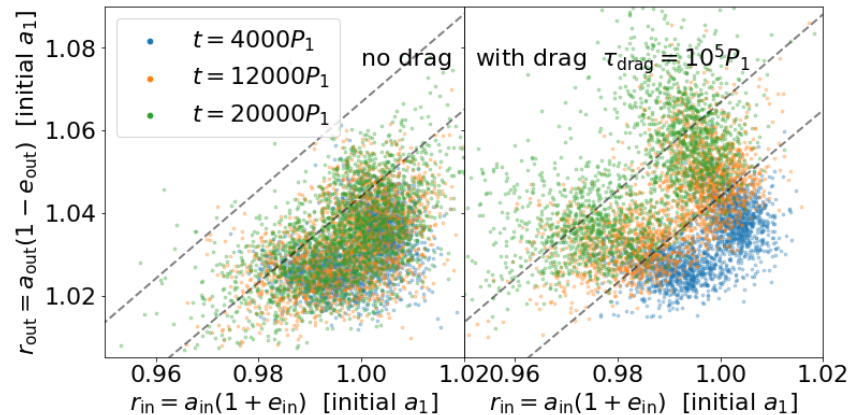
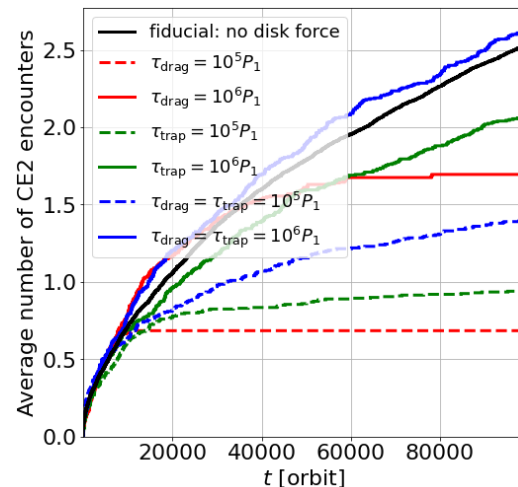
- Considered in our paper:

$$\mathbf{F}_{\text{drag}} = -\frac{\mathbf{v} - \mathbf{v}_K}{\tau_{\text{drag}}},$$

$$\mathbf{F}_{\text{trap}} = -\frac{\Omega_{K,0}(r - r_0)}{\tau_{\text{trap}}}\hat{\boldsymbol{\theta}},$$

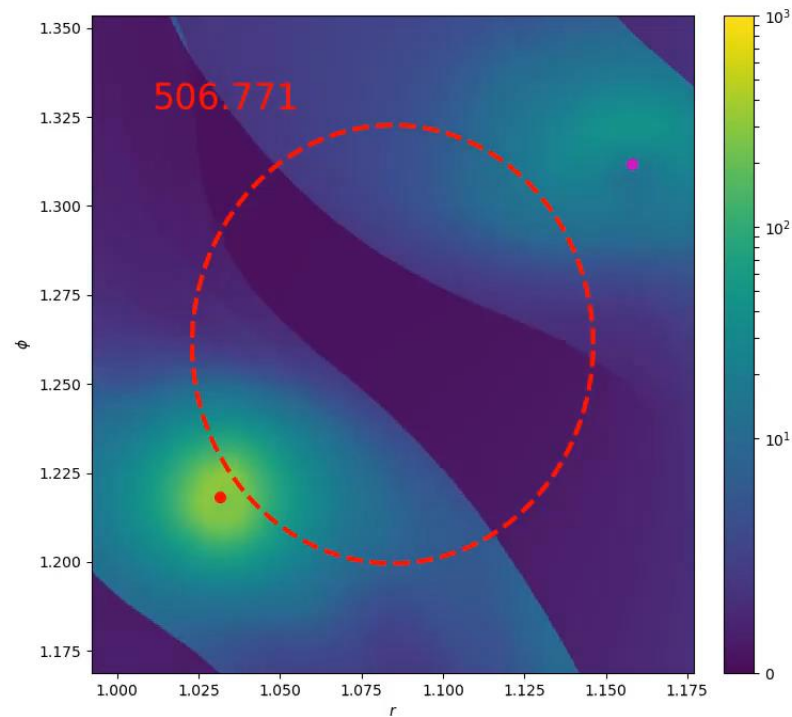
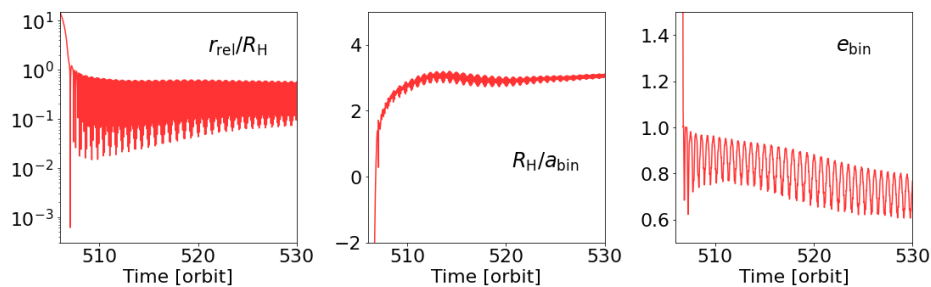
- They **do not** increase the GW capture rate.

(Li, Lai, and Rodet 2022, [arxiv:2203.05584](https://arxiv.org/abs/2203.05584))



# Dissipation through disk gas

- **Collisions between circum-stellar-BH disk** (ongoing work, Li et al. 2022 in prep).



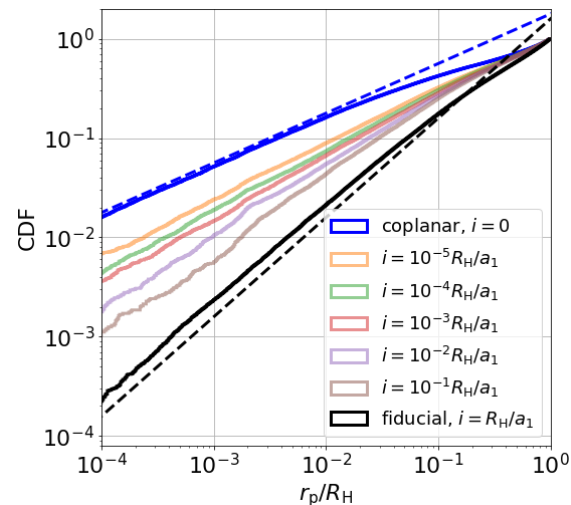
## Takeaways:

- Dynamical instability in AGN disks produces lots of CEs:
  - Without dissipation, CE pairs are **short-lived**.
  - Separation at CEs can be short enough for GW emission.
- GW radiation can **capture** BHs into binary:
  - Capture efficiency  $\sim N(t) \times \text{Prob}(r_p < r_{\text{cap}})$
  - Our average systems take  $\sim 10^8 P_1$  to get one GW capture.
- Check out our paper for more details (Li, Lai, & Rodet 2022, [arxiv:2203.05584](https://arxiv.org/abs/2203.05584)):
  - Gas effects; Parameter studies (mass, inclination, etc.); More explanations and discussions.

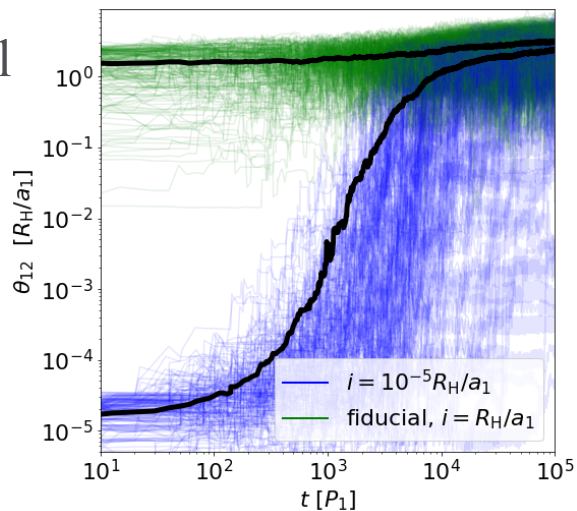
## Inclinations

- Exactly co-planar systems have the highest GW capture rate:  
 $\sim 10^8 P_1$  per capture
- However, exact co-planarity is not realistic because any non-zero small mutual inclination can grow.

(Li, Lai, and Rodet 2022, [arxiv:2203.05584](https://arxiv.org/abs/2203.05584))



Prob( $r_p$ ) changes with the mutual inclination.



Small mutual inclination converges to our fiducial inclination.