

# Formation of Black Hole Binaries in AGN disks through Close Encounters

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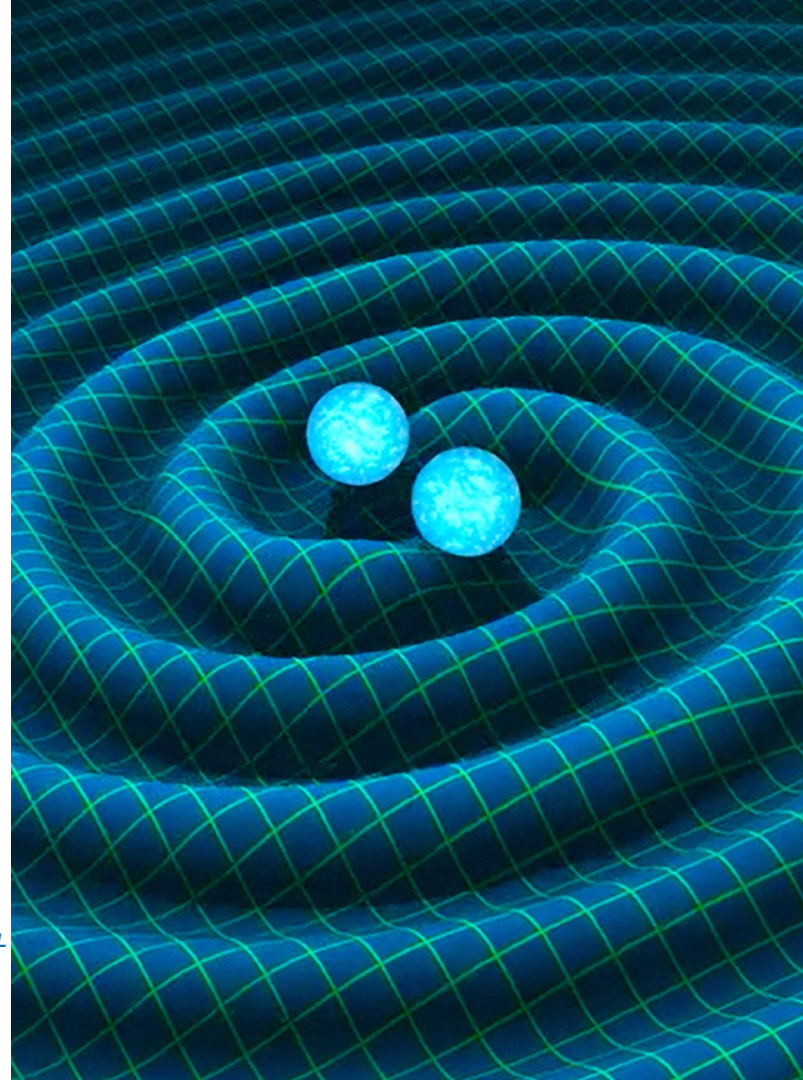
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J. Calcino (LANL), A. Dittmann (LANL), R. Li (Cornell),  
Ya-Ping Li (LANL→SHAO), B. Mishra (LANL)

# Why do we care about black hole (BH) binaries?

BH binaries are:

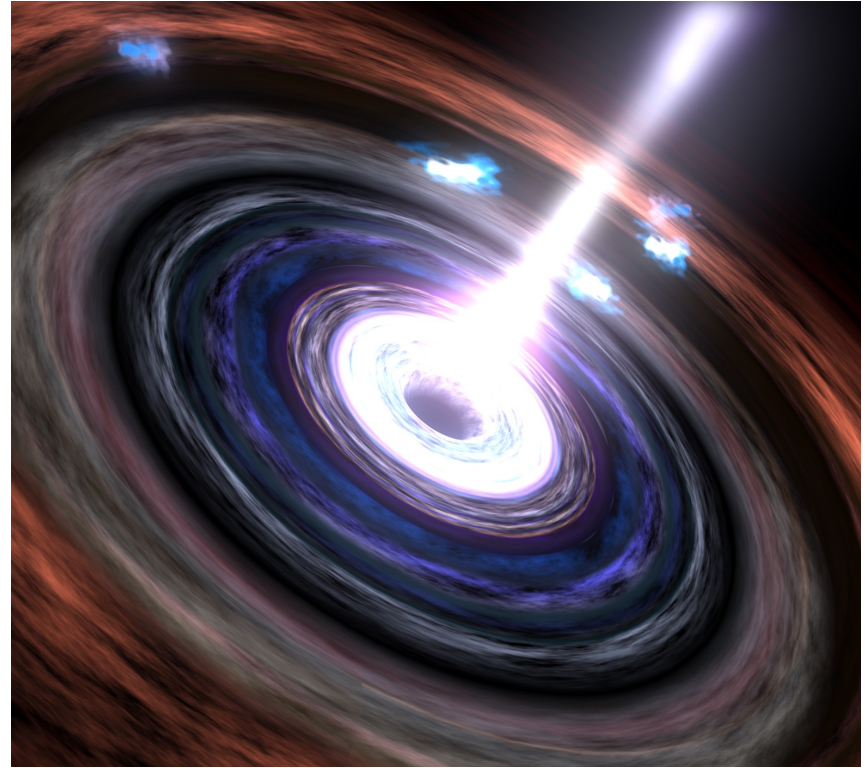
- the **simplest** systems that can produce significant gravitational wave (GW) signal,
- the **main** GW sources seen by LIGO (binary inspiral/merger).

*Image Credits: R. Hurt/Caltech-JPL*

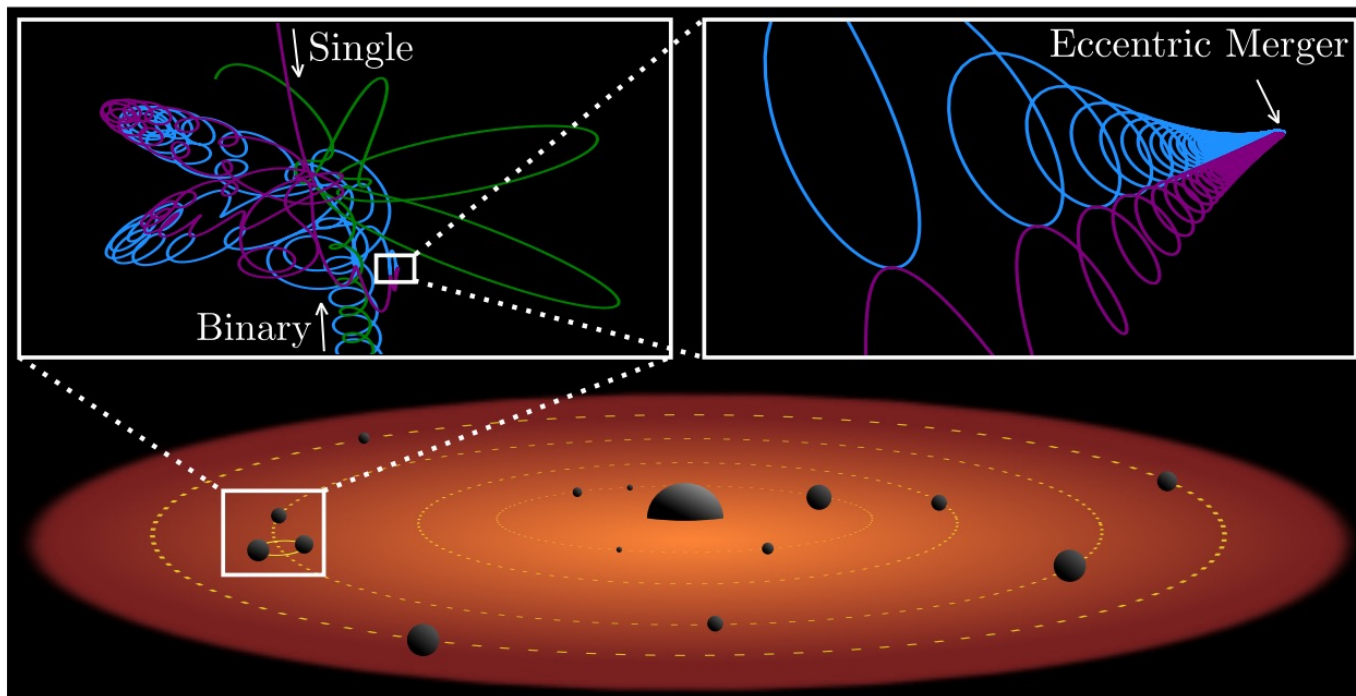


# Why do we care about BH binaries in AGN disks?

- GW radiation is weak when BHs are not very close to each other.  
→ No inspiral/mergers in Newtonian two-body problem.
- A binary embedded in a gaseous disk  
→ May be able to contract.

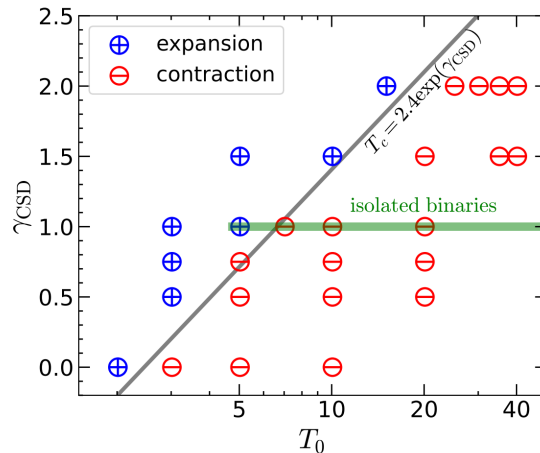
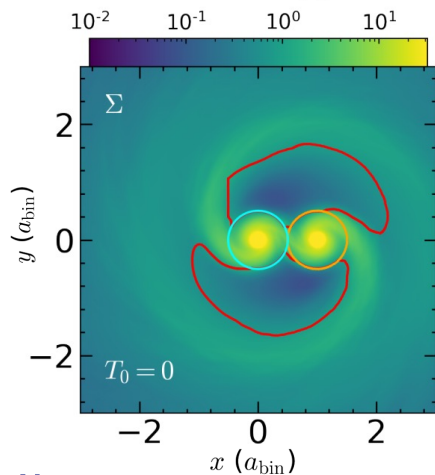
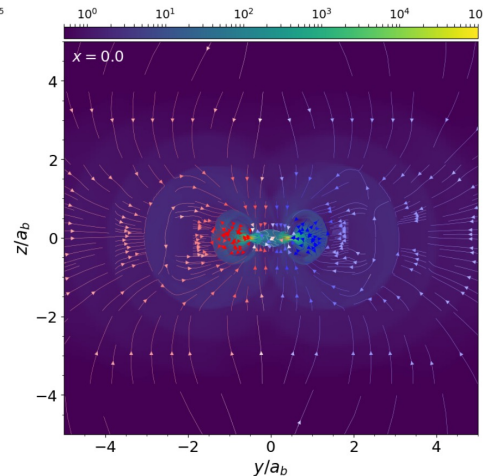
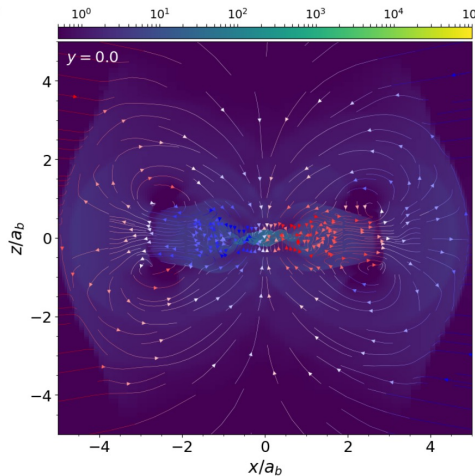
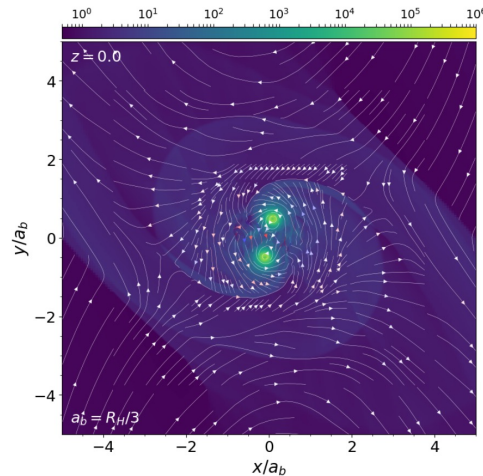


*Image Credits: NASA/GSFC Conceptual Image Lab*



Contraction of BH binaries due to scatterings  
(e.g., [Samsing et al. 2022](#)).



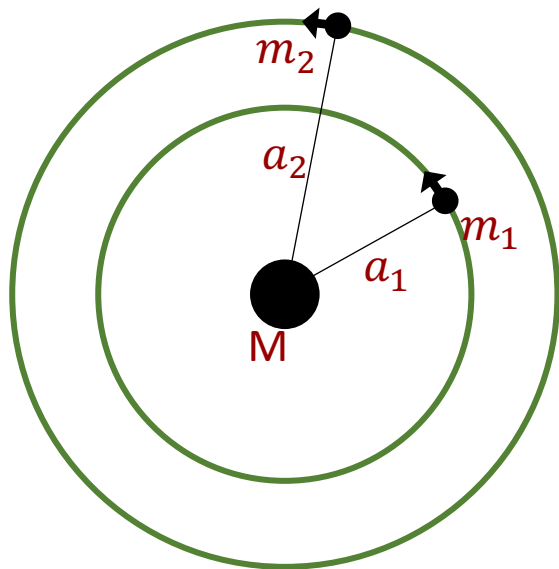


Contraction of BH binaries  
due to the surrounding gas  
(e.g., [Dempsey et al. 2022](#);  
[Li et al. incl. JL 2022](#)).

# We care about BH binaries in AGN disks..

- They may merge! (e.g., *Baruteau et al. 2011*; *Stone et al. 2017*; *Leigh et al. 2018*; *Li et al. incl. JL 2021, 2022*; *Dempsey et al. 2022*; *Li & Lai 2022a,b*; *Samsing et al. 2022*)
- However, almost all previous studies consider pre-existing binaries.
- **Q: How to form these BH binaries in AGN disks?**  
**A (in this talk): Close encounters between embedded single BHs.**

# Formation of BH binaries: long-term N-body simulations



- Initial condition:

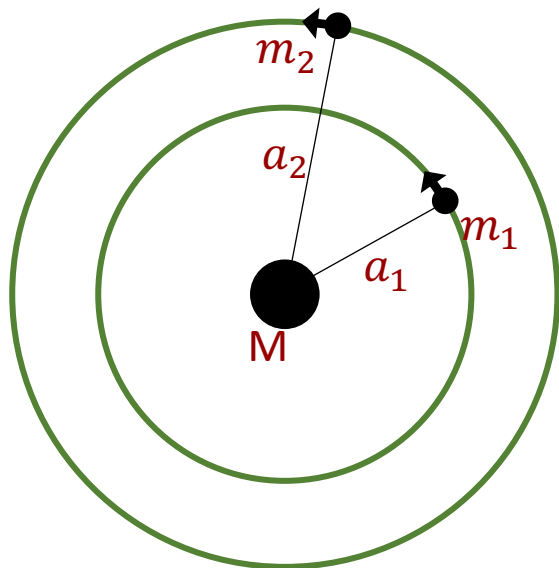
$$a_2 - a_1 = 2R_H \quad \text{where} \quad R_H = \frac{a_1 + a_2}{2} \left( \frac{m_1 + m_2}{3M} \right)^{1/3}$$

**(Dynamical instability will occur!)**

- Reasons for using closely-packed orbits:
  - Large BH population in an AGN disk
  - Differential migration
  - Focus on the close encounters

([Li, Lai, and Rodet 2022](#), [arxiv:2203.05584](#))

# Formation of BH binaries: long-term N-body simulations



- Simulations:
  - Run for at least  $10^5 P_1$  (orbits around the SMBH)
  - Pure N-body and **no gas effect** for now
- Outcomes of this instability:
  - BH collisions? -- unlikely
  - BH ejections? -- requires very long time
  - **Recurring close encounters** -- will be a lot!  
(we can study this stochastic process statistically)

([Li, Lai, and Rodet 2022](#), [arxiv:2203.05584](#))

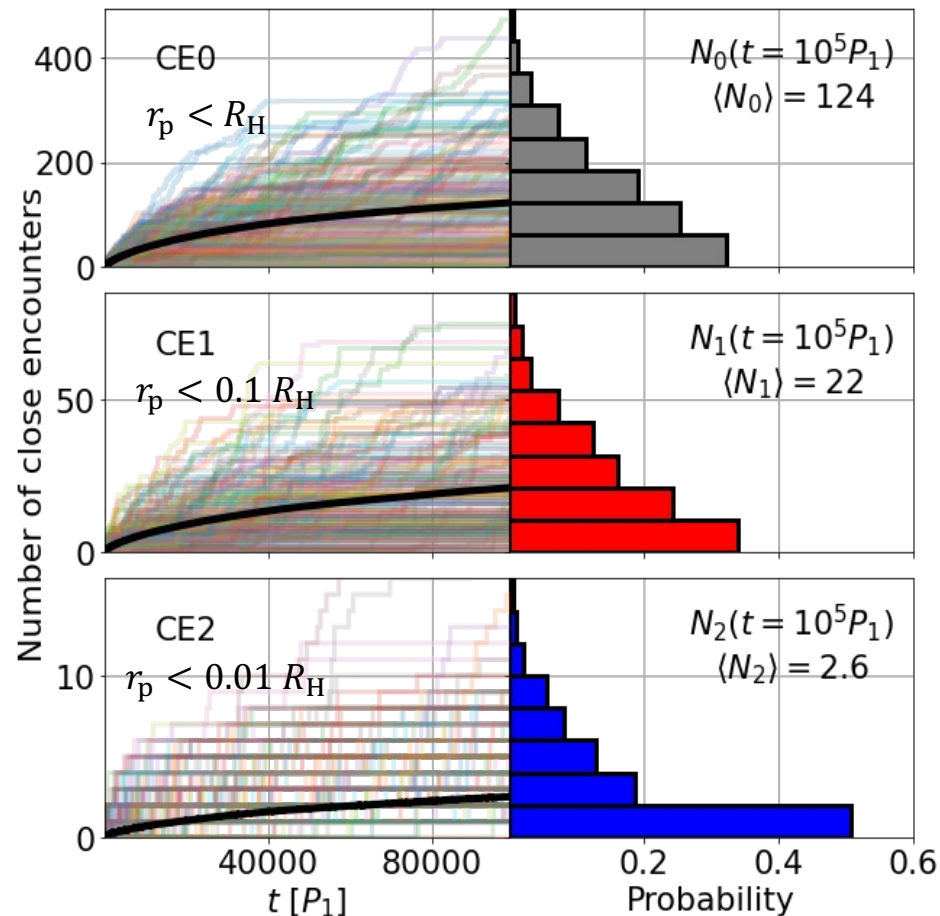


# N-body results

## Number of close encounters (CE)

$r_p$ : minimum BH separation during a CE

$P_1$ : orbital period around the SMBH



# N-body results

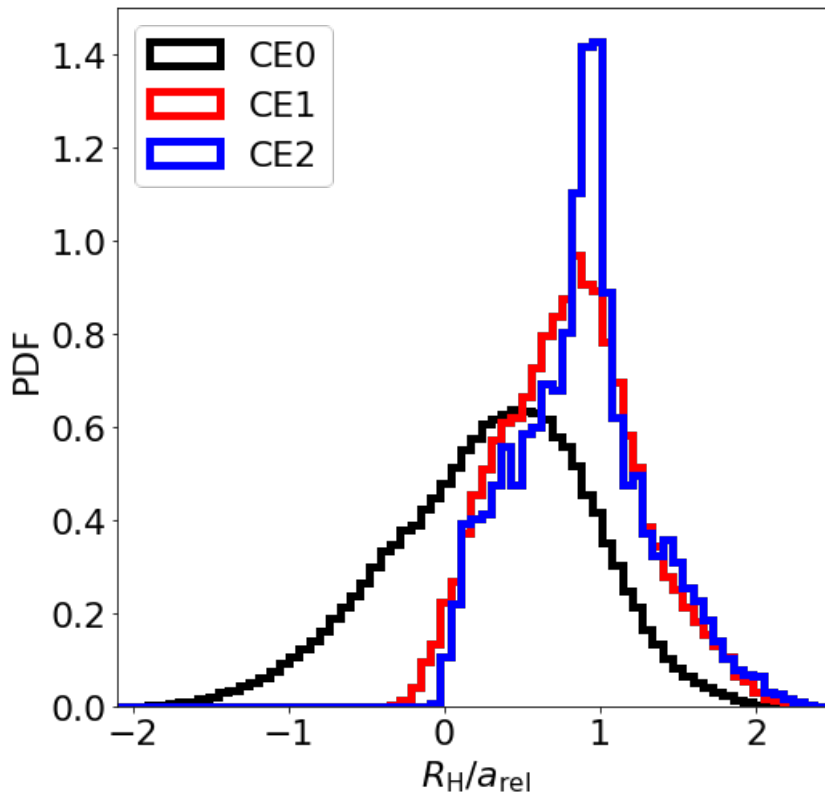
Energy of a CE:

$$E = -\frac{Gm_1m_2}{2a_{\text{rel}}} = \frac{1}{2}\mu v_{\text{rel}}^2 - \frac{Gm_1m_2}{r_{\text{rel}}}$$

'Stability' of a CE:

$$R_{\text{H}}/a_{\text{rel}} = \frac{Gm_1m_2}{2a_{\text{rel}}} / \frac{Gm_1m_2}{2R_{\text{H}}}$$

Most encountering BH pairs are disrupted by the **SMBH tidal force** within  $1 P_1$ .



# Reduce CE energy through GW radiation

- BHs can be captured into long-lived binary if enough energy is radiated **at once**:

$$\Delta E_{\text{GW}} = \frac{85\pi}{12\sqrt{2}} \frac{G^{7/2} \mu^2 m_{12}^{5/2}}{c^5 r_p^{7/2}} \quad \gtrsim \eta \frac{G m_1 m_2}{R_{\text{H}12}}$$

energy radiated by GW  
(Quinlan & Shapiro 1989)

energy needs to be  
removed for binding

- $r_p$  needs to be smaller than a critical capture radius:

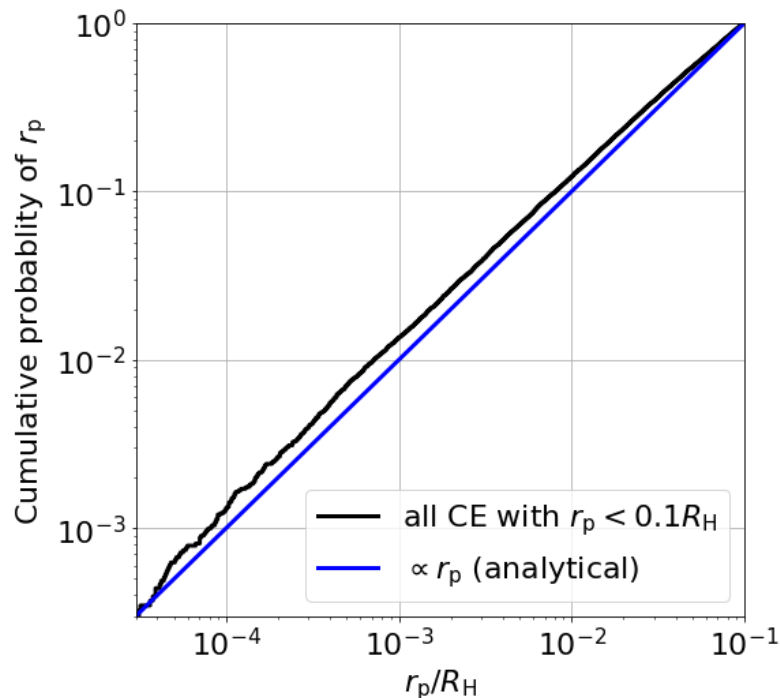
$$\frac{r_p}{R_H} < \frac{r_{\text{cap}}}{R_H} \simeq 10^{-4} \left( \frac{4\mu}{m_{12}} \right)^{\frac{2}{7}} \left( \frac{10^6 m_{12}}{M} \right)^{\frac{10}{21}} \left( \frac{a_{\text{SMBH}}}{100 GM/c^2} \right)^{-5/7}$$

# Reduce CE energy through GW radiation

- $r_p$  needs to be smaller than the critical capture radius:

$$\frac{r_p}{R_H} < \frac{r_{\text{cap}}}{R_H} \simeq 10^{-4}$$

- We show numerically and analytically that  $r_p$  follows a power-law cumulative probability distribution, which allows  $r_p$  to be arbitrarily small.

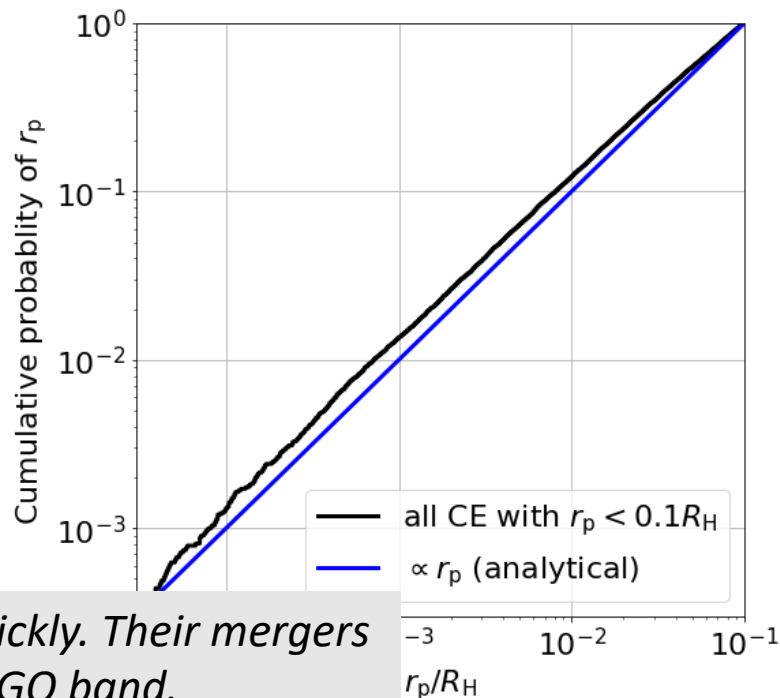


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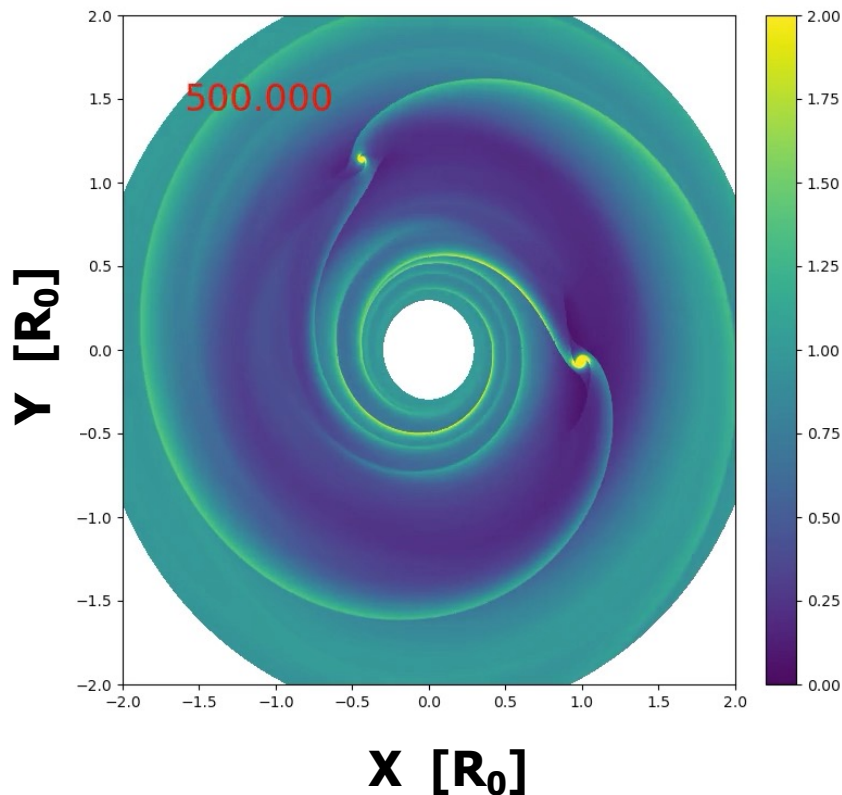
*\* We expect these captured binaries to merge quickly. Their mergers will show **high eccentricities** when entering the LIGO band.*

# Takeaways from N-body results

- Dynamical instability in AGN disks produces lots of CEs:
  - Without dissipation, CE pairs are **short-lived**.
  - Separation at CEs can be short enough for GW emission.
- GW radiation can **capture** BHs into binary:
  - With a very small probability  $\sim \frac{r_{\text{cap}}}{R_H} \ll 1$ .
  - These captured binaries should merge very quickly.



# Formation of BH binaries: hydrodynamics simulations



- Initial condition:

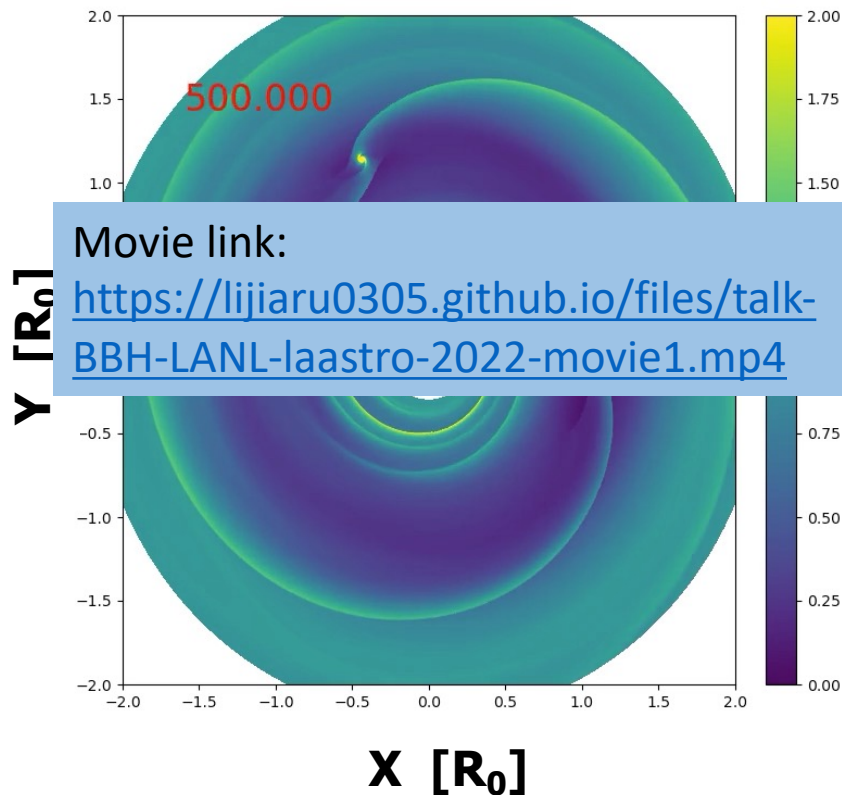
$$a_2 - a_1 = 2R_H$$

(Close encounter at the first conjunction)

- Simulation setup:

- $M_{\text{SMBH}} = 1$ ,  $m_1 = 10^{-5}$ ,  $m_2 = 5 \times 10^{-6}$
- Thin disk  $H/R = 0.01$ , low viscosity  $\alpha = 0.01$ .
- Isothermal disk.
- High resolution with 100 grid cells per  $R_H$ , where  $R_H = 0.017R_0$

# Formation of BH binaries: hydrodynamics simulations



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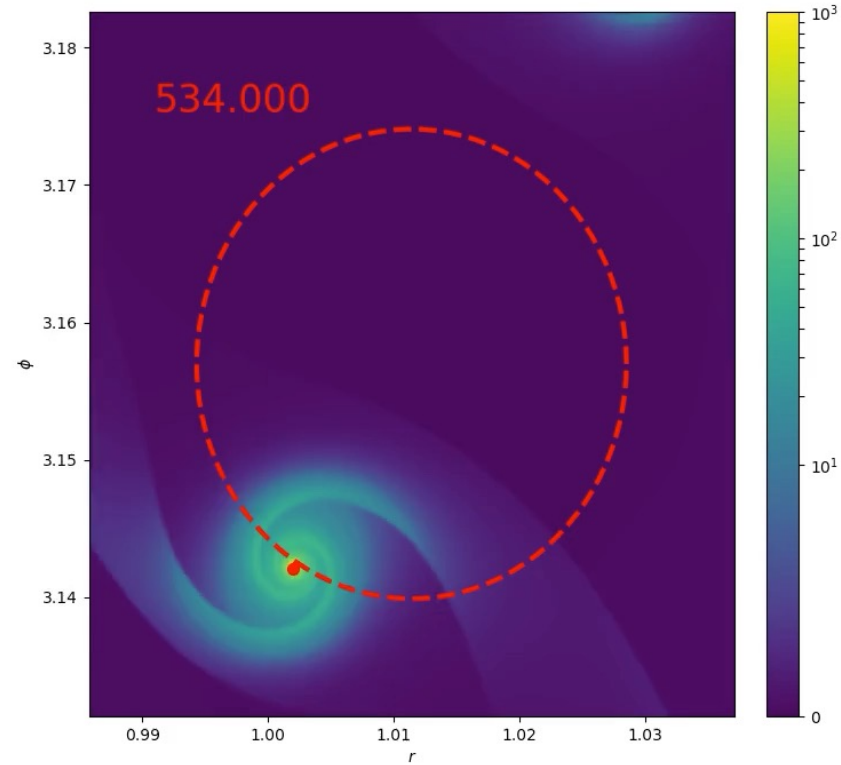
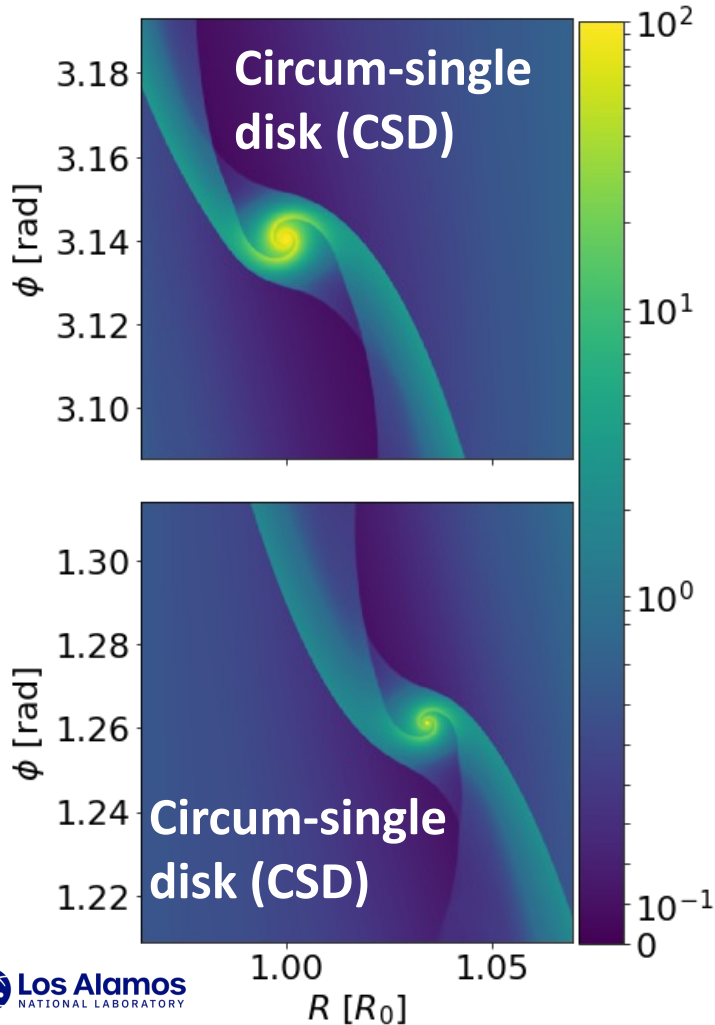
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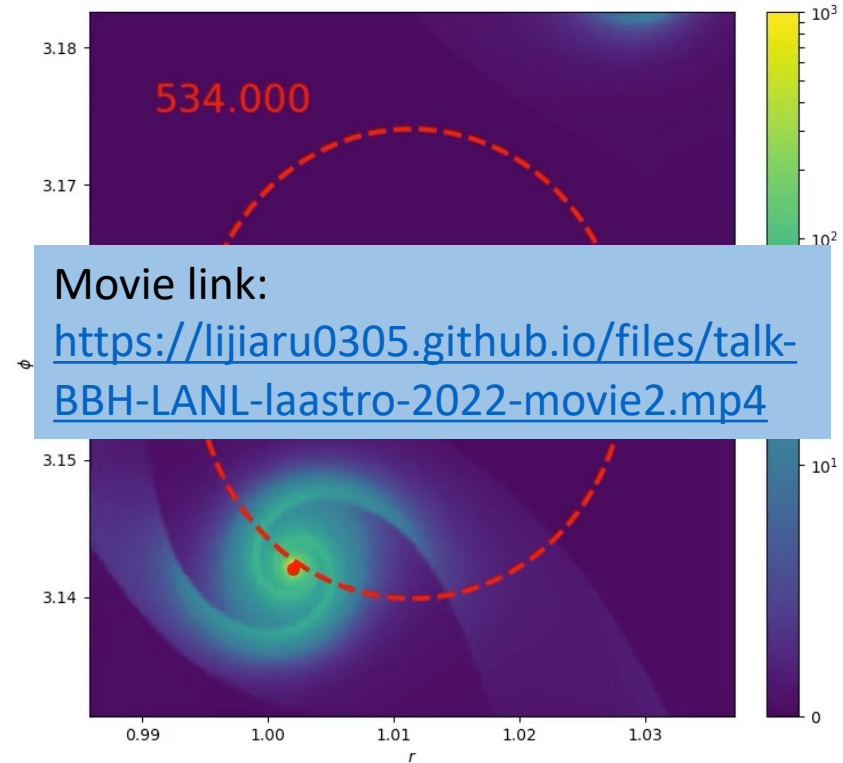
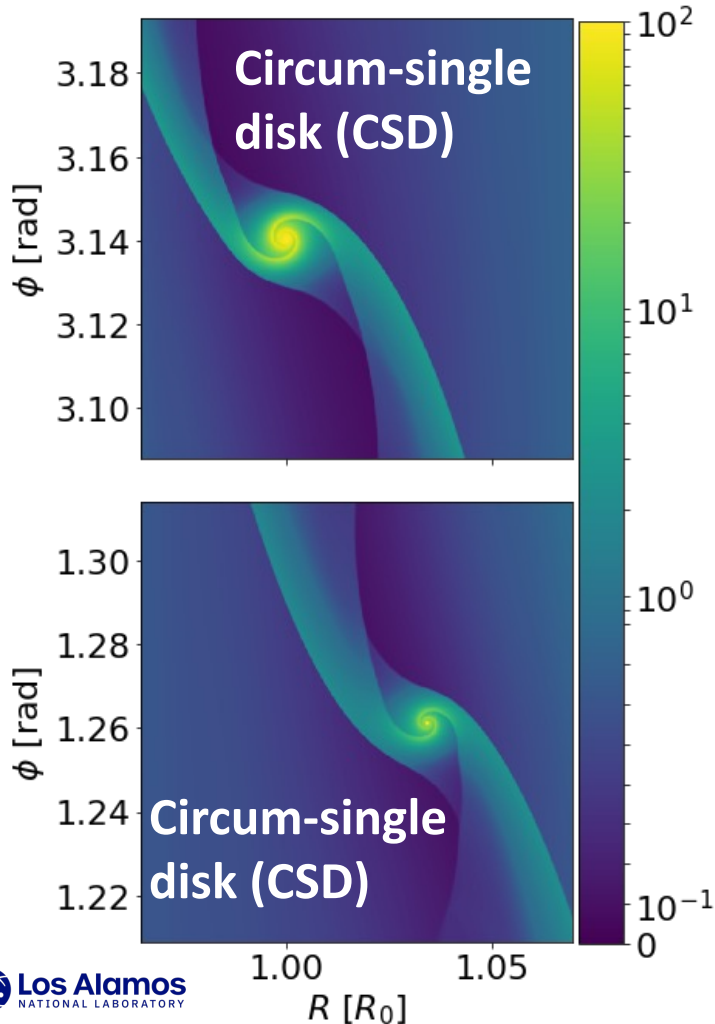
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## Formation process

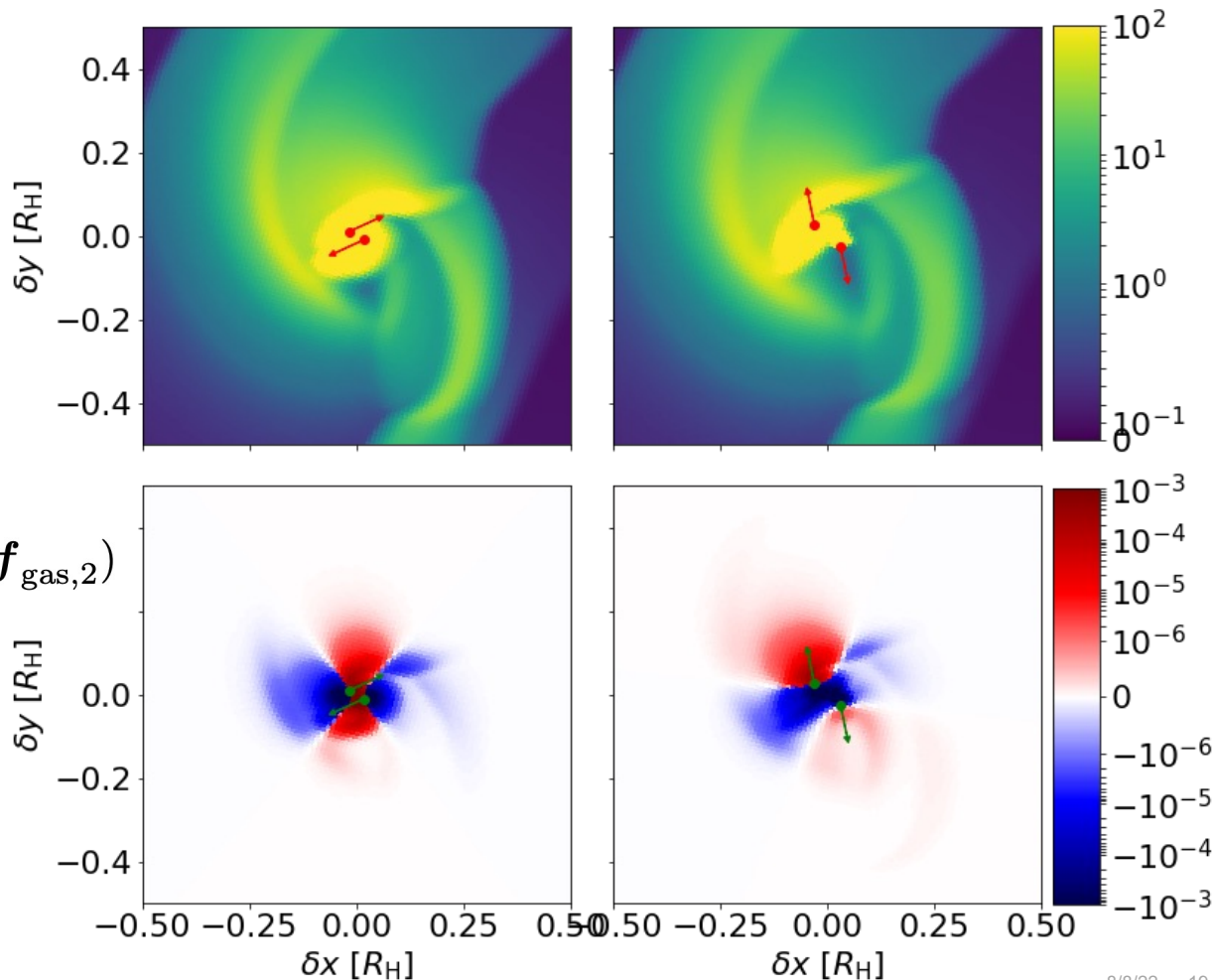


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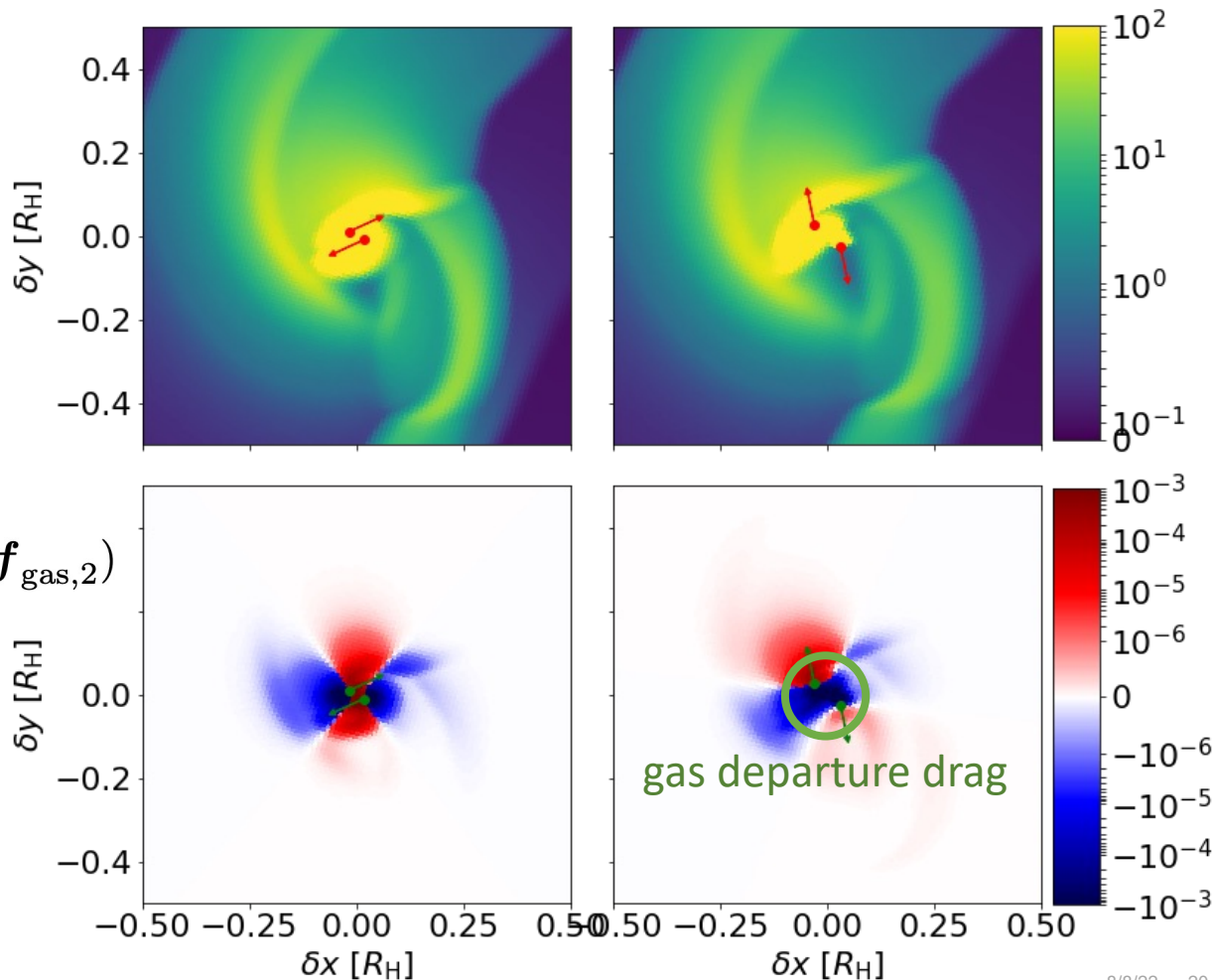
# Energy change rate of the binary due to gas gravity

$$\dot{E}_{\text{gas}} = \mu(\mathbf{v}_1 - \mathbf{v}_2) \cdot (\mathbf{f}_{\text{gas},1} - \mathbf{f}_{\text{gas},2})$$



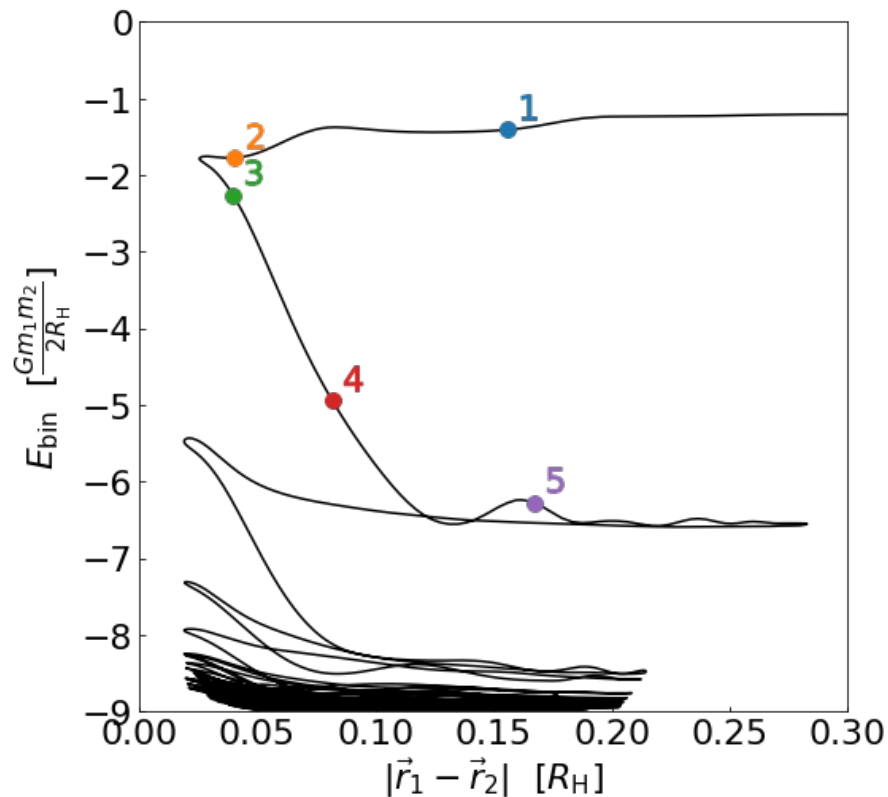
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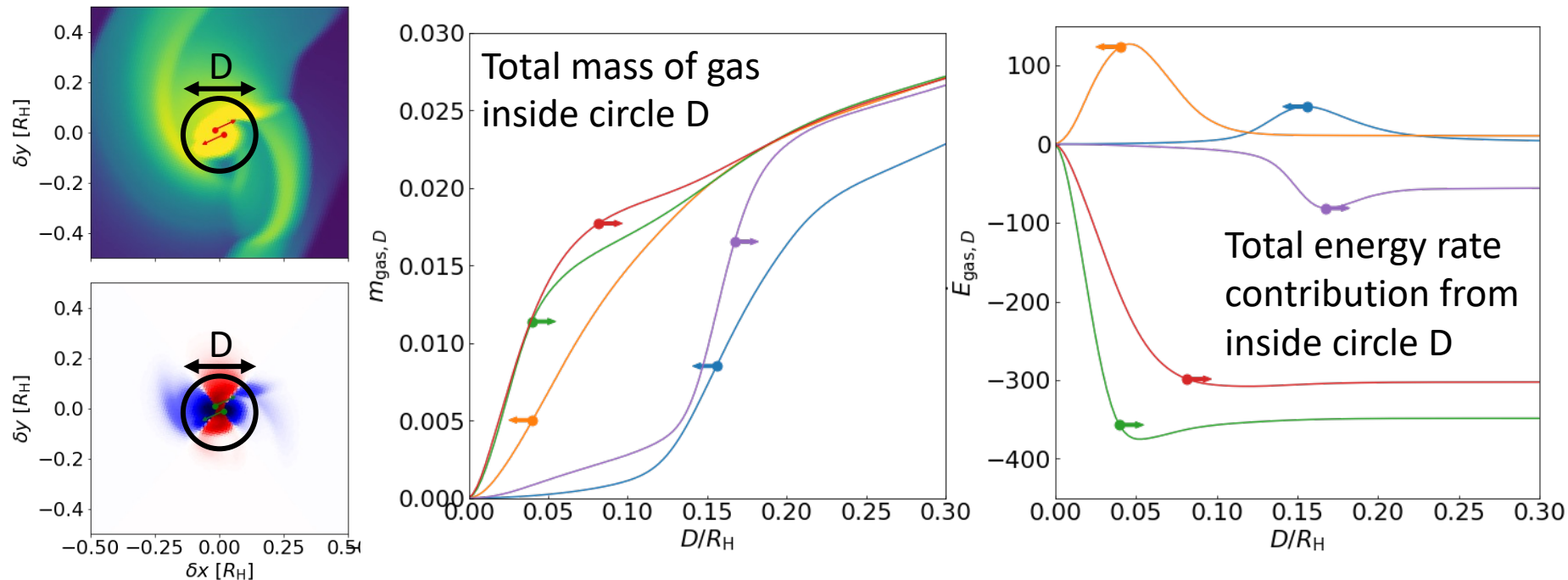
# Analysis of the departure drag



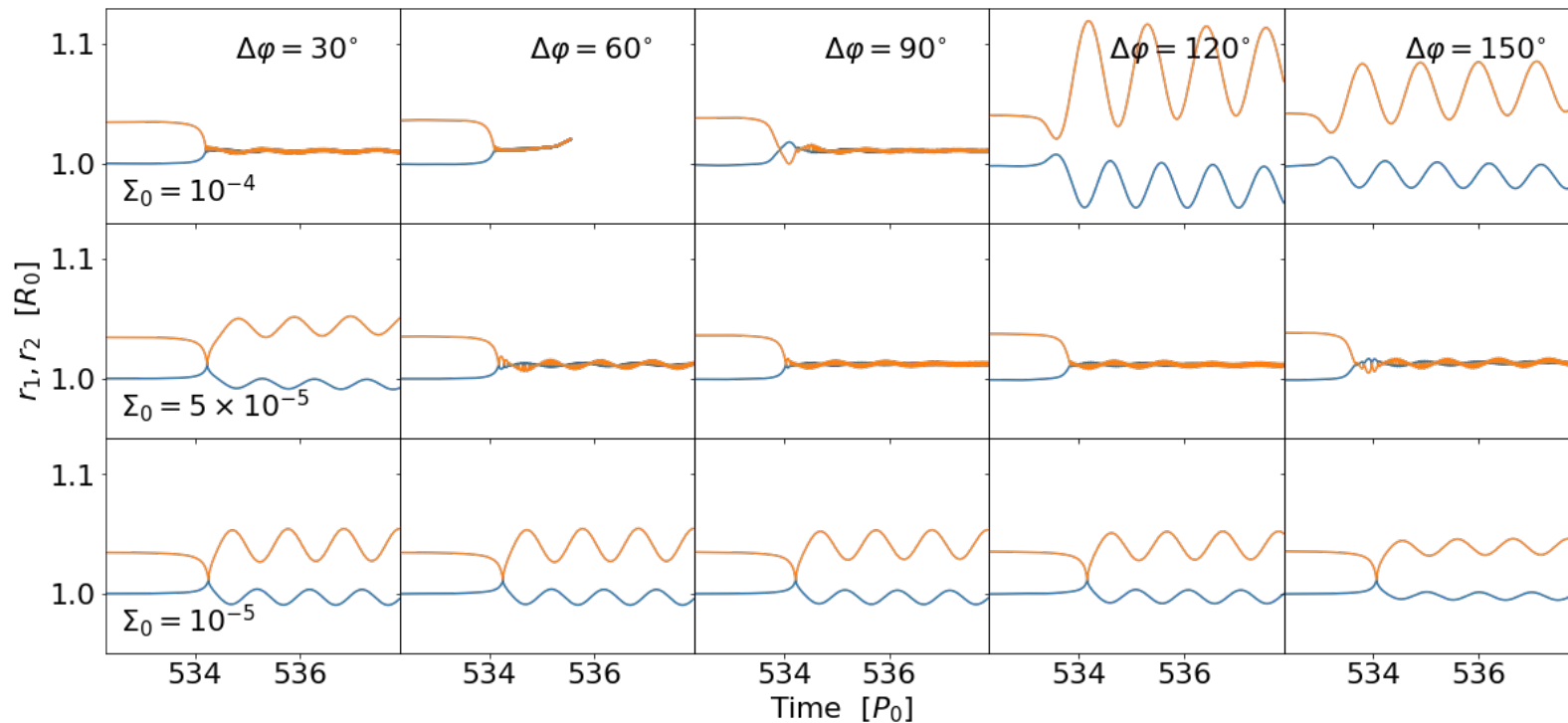
Time evolution of BHs in the parameter space of the binary relative energy ( $E_{\text{bin}}$ ) and separation ( $|r_{\text{rel}}| = |r_1 - r_2|$ ).

$$E_{\text{bin}} = \frac{1}{2}\mu v_{\text{rel}}^2 - \frac{Gm_1m_2}{r_{\text{rel}}}$$

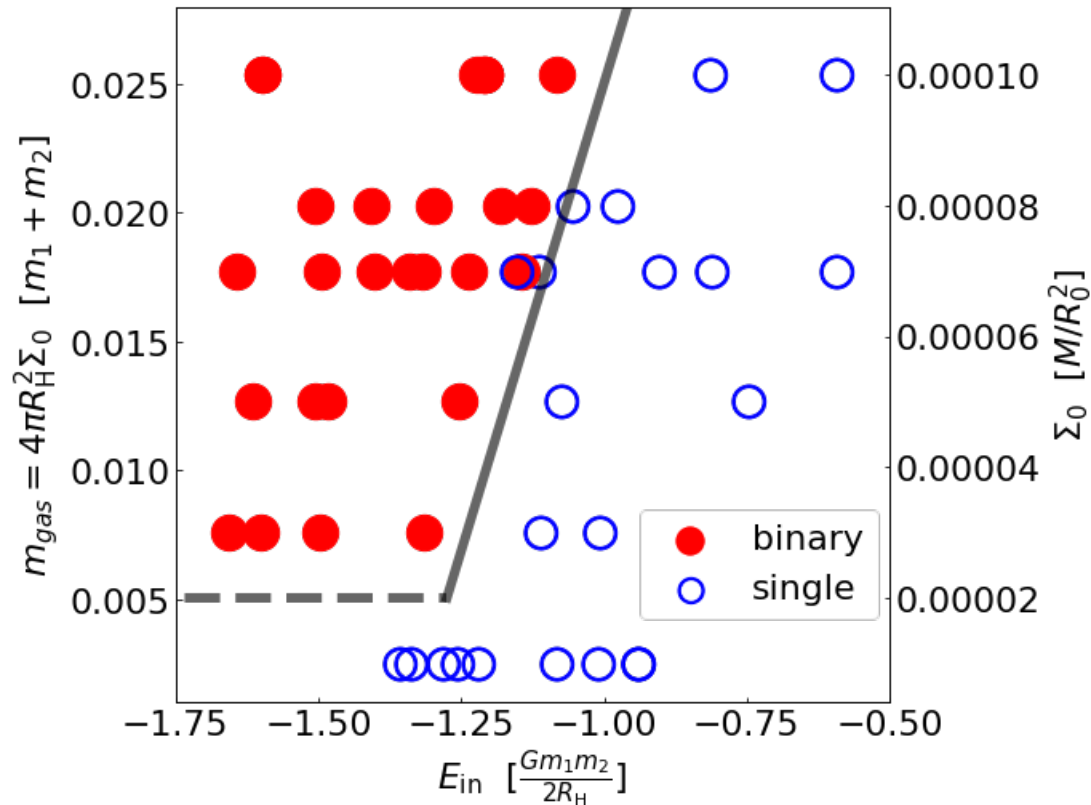
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# Parameter space for binary formation



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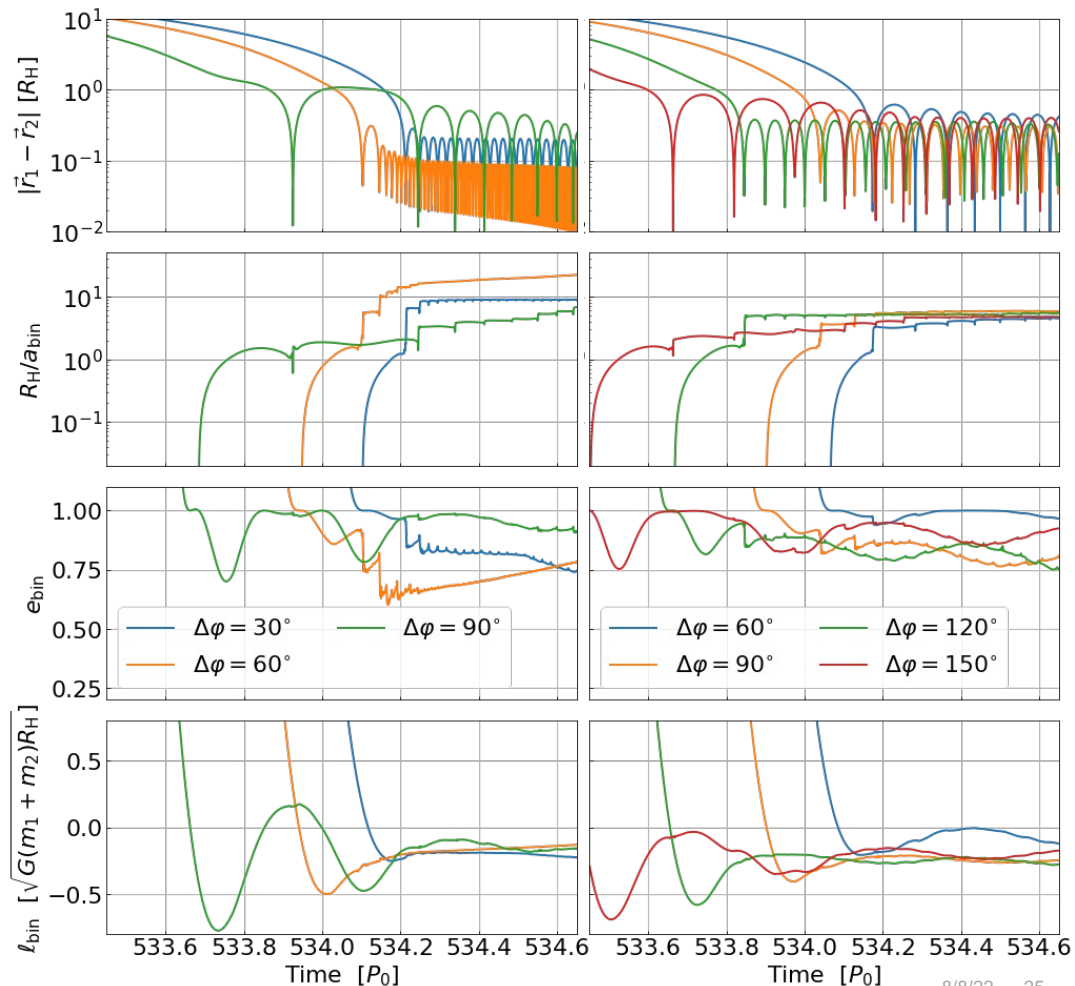
$E_{\text{in}} := E_{\text{bin}} \mid \text{before pericenter}$

Forming binary requires:

- sufficiently large gas mass
- sufficiently small initial binary energy

# Resulted binary orbit after formation

- small semi-major axis:  $\frac{a_{\text{bin}}}{R_H} \sim 0.1$
- large eccentricity:  $e_{\text{bin}} > 0.5$
- retrograde rotation:  $\ell_{\text{bin}} < 0$



# Summary

- Mergers of BH binaries embedded in AGN disks are considered important sources of gravitational wave.
- In the low gas density limit, dynamical instability produces lots of close encounters. → In rare events of every deep encounters, very tightly-bounded GW-dominated binaries can form.
- When the gas density is sufficiently high, close encounters can form bound binaries due to the collision between the two CSDs. → Formation-per-encounter ratio is much higher than in the low density limit.
- The resulted BH binary orbits can be highly eccentric, compact, and retrograde.