

# Formation of Black Hole Binaries in AGN disks through Close Encounters

Jiaru Li (Cornell)

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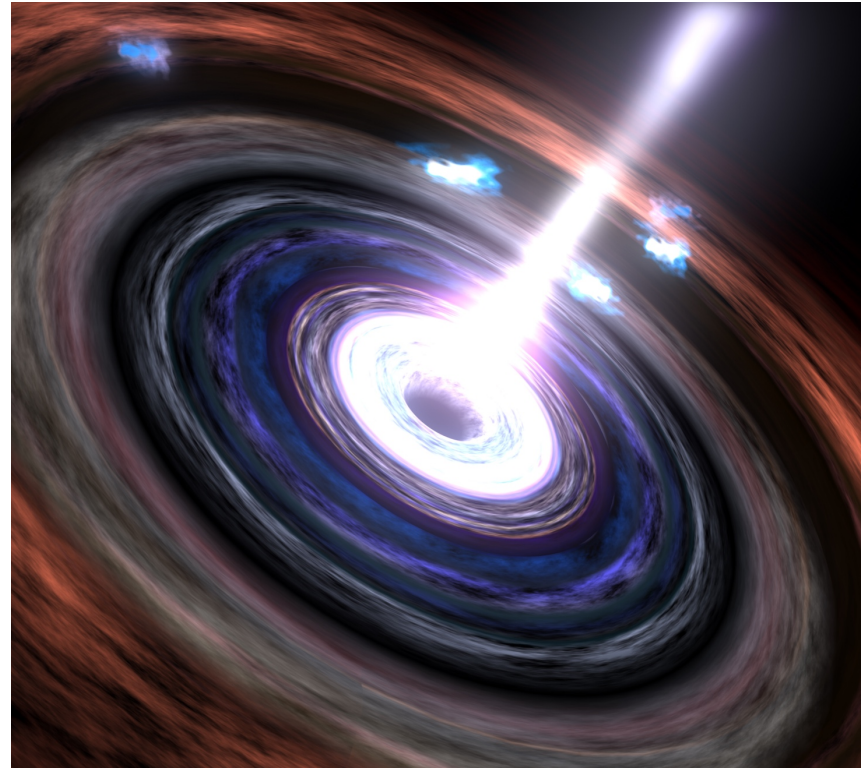
Collaborators of this project:

Dong Lai and Laetitia Rodet (Cornell)

Hui Li, Adam Dempsey and Shengtai Li (LANL)

## Why do we care about BH binaries in AGN disks?

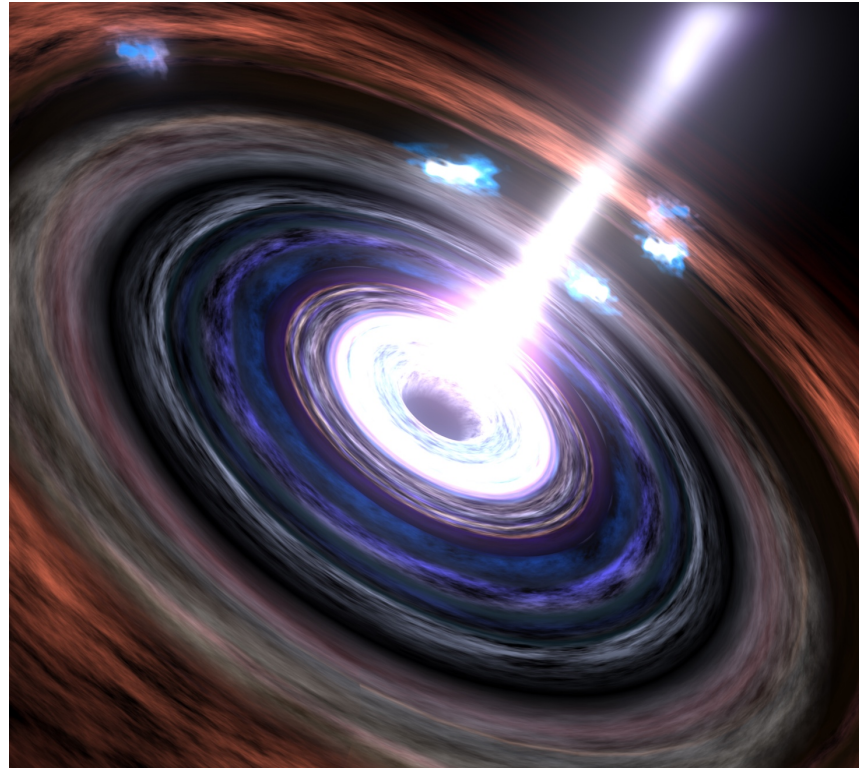
- Mergers in AGN disks may have distinct observable distribution of mass, spin, and eccentricity (e.g., *McKernan+ 2018; Yang+ 2019; Gerosa & Fishbach 2021; Li+2022*).
- Mergers may also produce electromagnetic counterparts (e.g., *Stone+ 2017; McKernan+ 2019; Graham+ 2020*).



*Image Credits: NASA/GSFC Conceptual Image Lab*

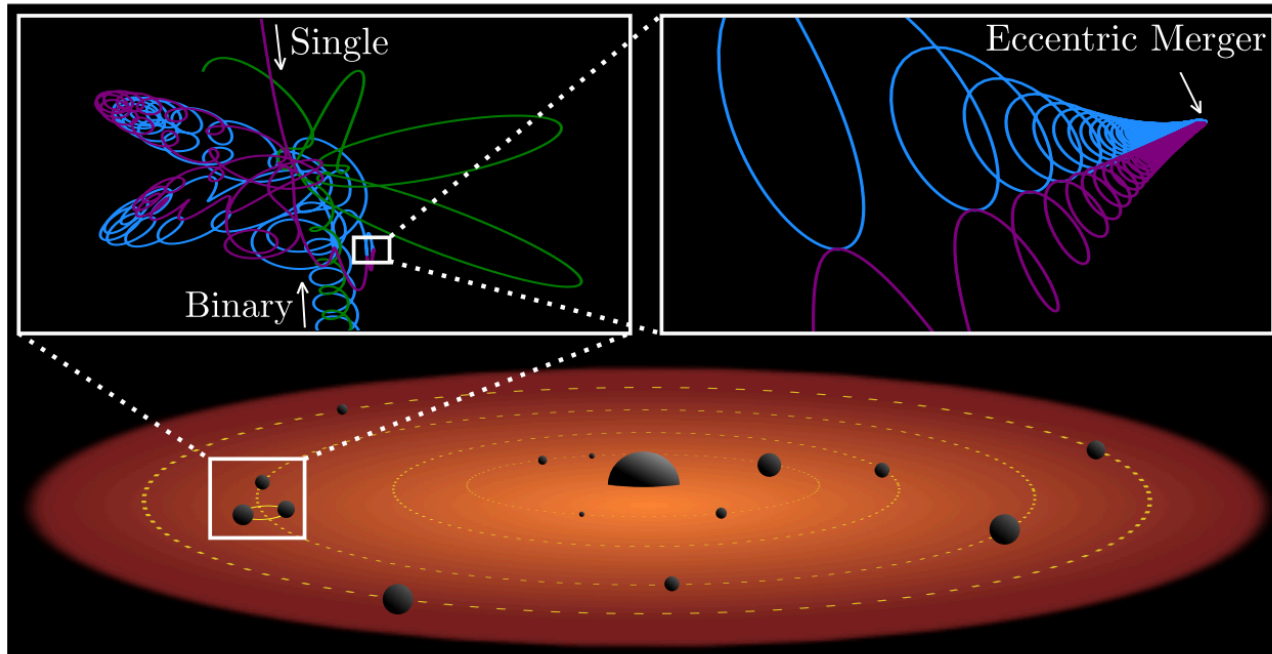
## Why do we care about BH binaries in AGN disks?

- AGN disks may **assist** the BH binaries to evolve toward their mergers.



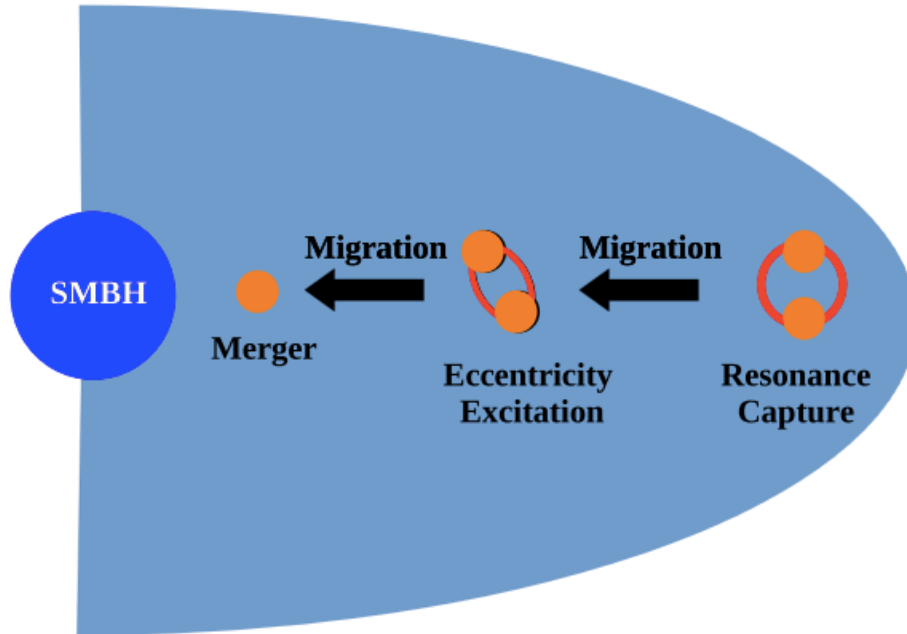
*Image Credits: NASA/GSFC Conceptual Image Lab*

# Mechanisms to merge an embedded binary..



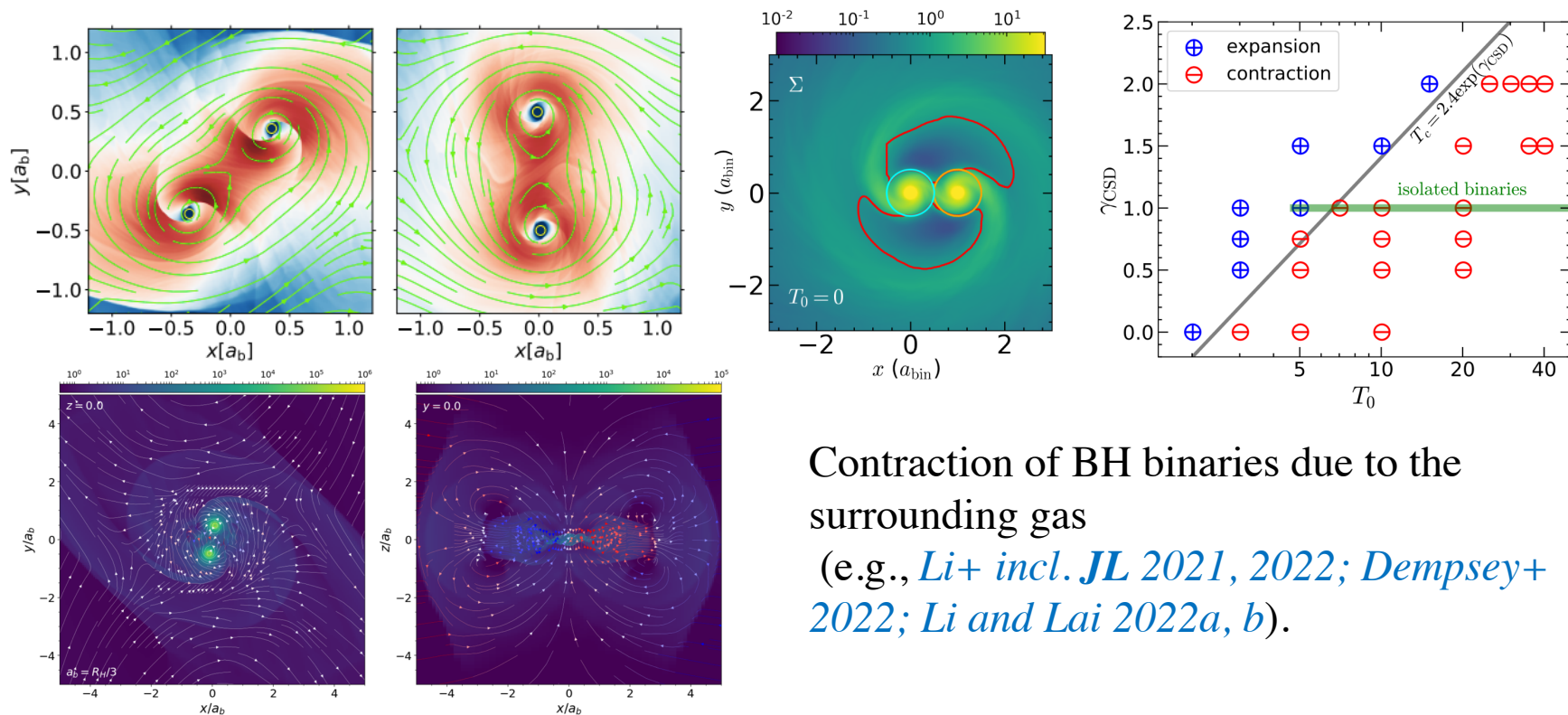
Contraction of BH binaries due to scatterings  
(e.g., *Leigh+ 2018; Samsing+ 2022*).

# Mechanisms to merge an embedded binary..



Eccentricity excitation due to evection resonances  
(e.g., *Bhaskar+ 2022*; *Muñoz+ 2022*).

# Mechanisms to merge an embedded binary..



Contraction of BH binaries due to the surrounding gas

(e.g., *Li+ incl. JL 2021, 2022; Dempsey+ 2022; Li and Lai 2022a, b*).

## about BH binaries in AGN disks...

- They may merge! (e.g., *Baruteau+ 2011; Stone+ 2017; Leigh+ 2018; Li+ incl. JL 2021, 2022; Dempsey et al. 2022; Li & Lai 2022a,b; Samsing et al. 2022*)

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- However, almost all previous studies consider pre-existing binaries.
- **Q: How to form these BH binaries in AGN disks?**

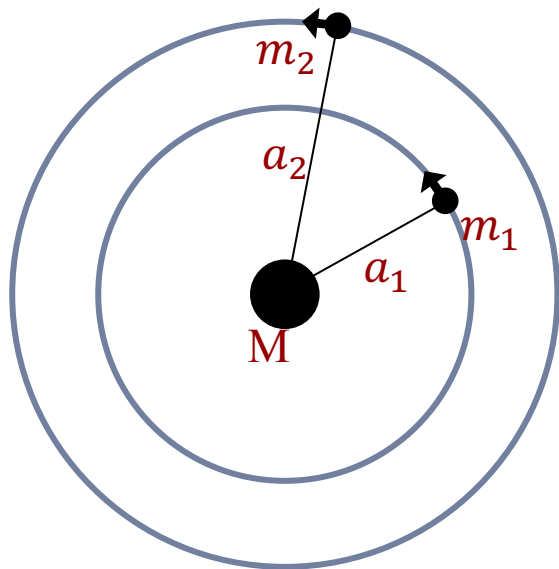


## about BH binaries in AGN disks...

- They may merge! (e.g., *Baruteau+ 2011; Stone+ 2017; Leigh+ 2018; Li+ incl. JL 2021, 2022; Dempsey et al. 2022; Li & Lai 2022a,b; Samsing et al. 2022*)
- However, almost all previous studies consider pre-existing binaries.
- **Q: How to form these BH binaries in AGN disks?**  
**A (in this talk): Close encounters between embedded single BHs.**

# Formation of BH binaries: long-term N-body simulations

(Li, Lai, and Rodet 2022)



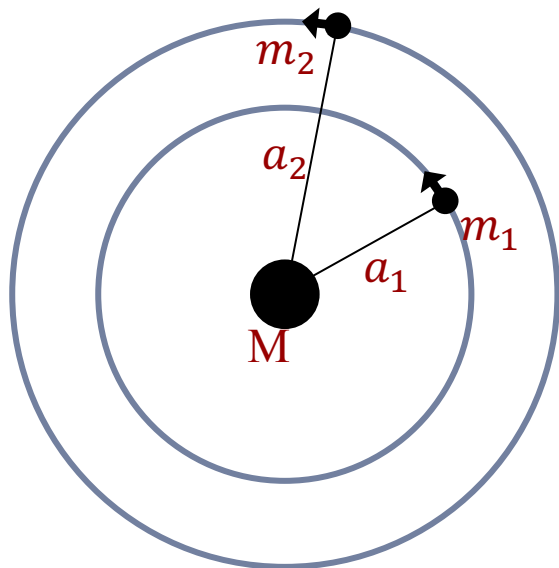
- Initial condition:

$$a_2 - a_1 = 2R_H \quad \text{where} \quad R_H = \frac{a_1 + a_2}{2} \left( \frac{m_1 + m_2}{3M} \right)^{1/3}$$

**(Dynamical instability will occur!)**

- Reasons for using closely-packed orbits:
  - Large BH population in an AGN disk
  - Differential migration
  - Focus on the close encounters

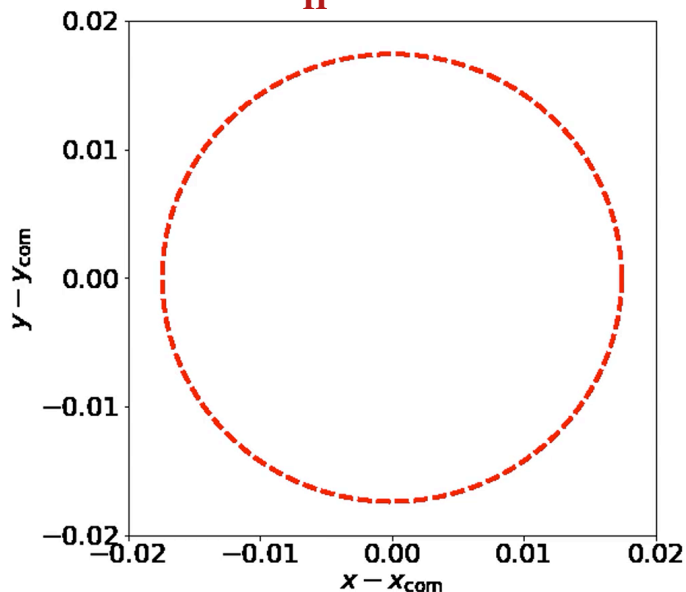
# Formation of BH binaries: long-term N-body simulations



- Simulations:
  - Run for at least  $10^5 P_1$  (orbits around the SMBH)
  - Pure N-body and **no gas effect** for now
- Outcomes of this instability:
  - BH collisions? -- unlikely
  - BH ejections? -- requires very long time
  - **Recurring close encounters** -- will be a lot!  
(we can study this stochastic process statistically)

# Formation of BH binaries: long-term N-body simulations

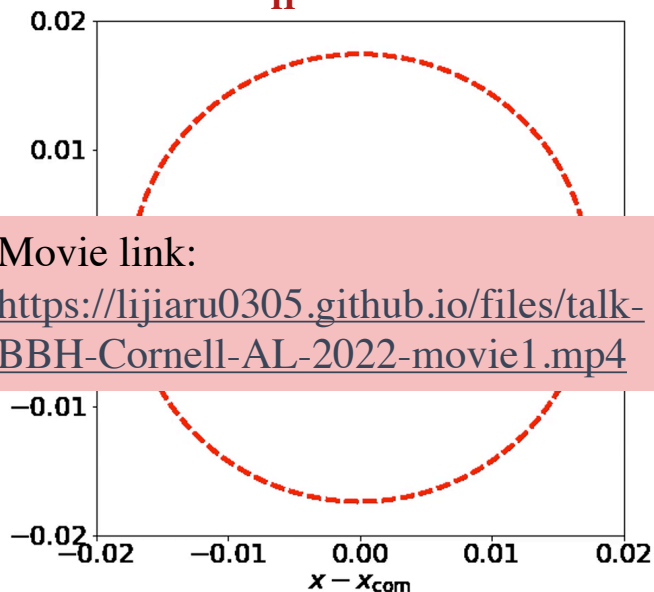
## Radius $R_H$ at the BH COM



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# Formation of BH binaries: long-term N-body simulations

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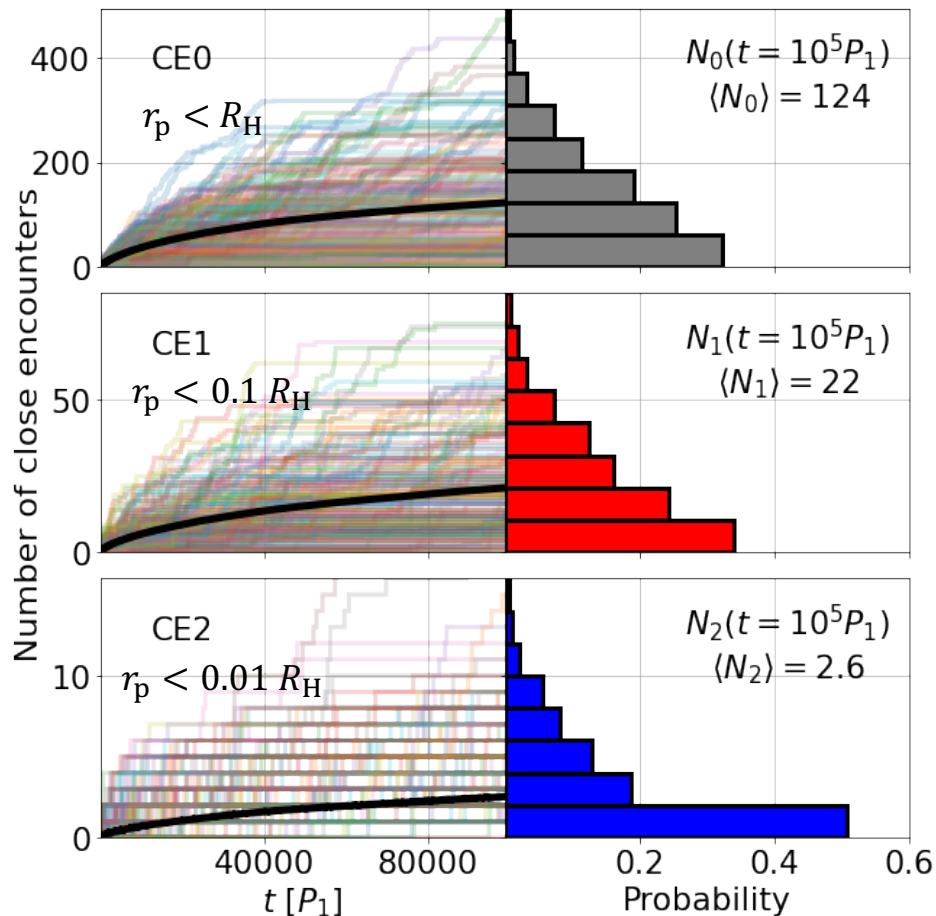
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# N-body results

## Number of close encounters (CE)

$r_p$ : minimum BH separation during a CE

$P_1$ : orbital period around the SMBH



# N-body results

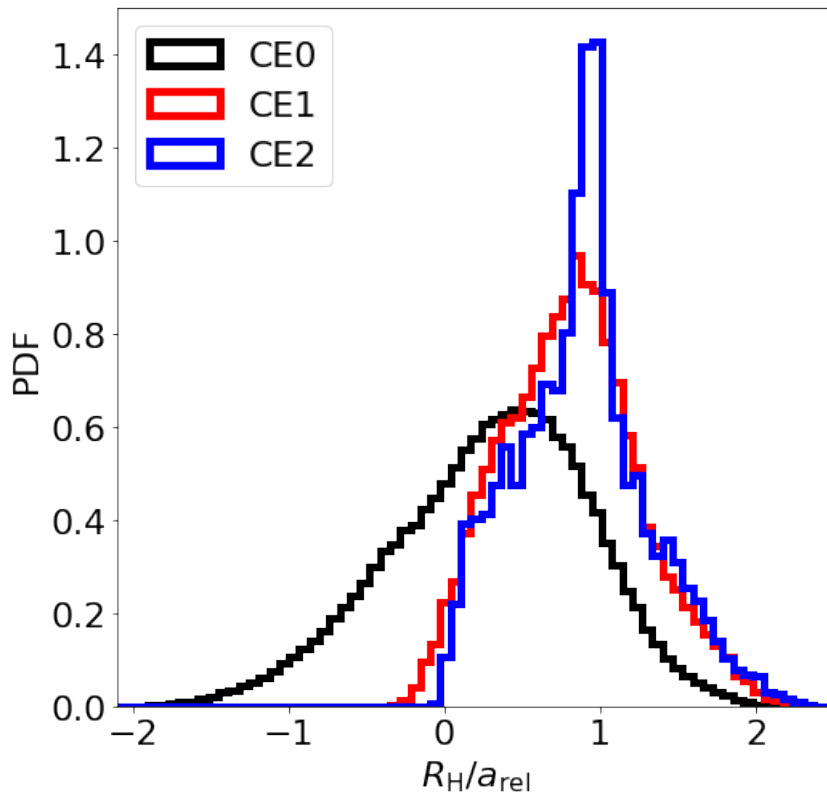
Energy of a CE:

$$E = -\frac{Gm_1m_2}{2a_{\text{rel}}} = \frac{1}{2}\mu v_{\text{rel}}^2 - \frac{Gm_1m_2}{r_{\text{rel}}}$$

'Stability' of a CE:

$$R_{\text{H}}/a_{\text{rel}} = \frac{Gm_1m_2}{2a_{\text{rel}}} / \frac{Gm_1m_2}{2R_{\text{H}}}$$

Most encountering BH pairs are disrupted by the **SMBH tidal force** within  $1 P_1$ .



# Reduce CE energy through GW radiation

- BHs can be captured into long-lived binary if enough energy is radiated **at once**:

$$\Delta E_{\text{GW}} = \frac{85\pi}{12\sqrt{2}} \frac{G^{7/2} \mu^2 m_{12}^{5/2}}{c^5 r_p^{7/2}} \quad \gtrsim \eta \frac{Gm_1 m_2}{R_{\text{H}12}}$$

**energy radiated by GW**  
*(Quinlan & Shapiro 1989)*

**energy needs to be removed for binding**

- $r_p$  needs to be smaller than a critical capture radius:

$$\frac{r_p}{R_{\text{H}}} < \frac{r_{\text{cap}}}{R_{\text{H}}} \simeq 10^{-4} \left( \frac{4\mu}{m_{12}} \right)^{\frac{2}{7}} \left( \frac{10^6 m_{12}}{M} \right)^{\frac{10}{21}} \left( \frac{a_{\text{SMBH}}}{100GM/c^2} \right)^{-5/7}$$

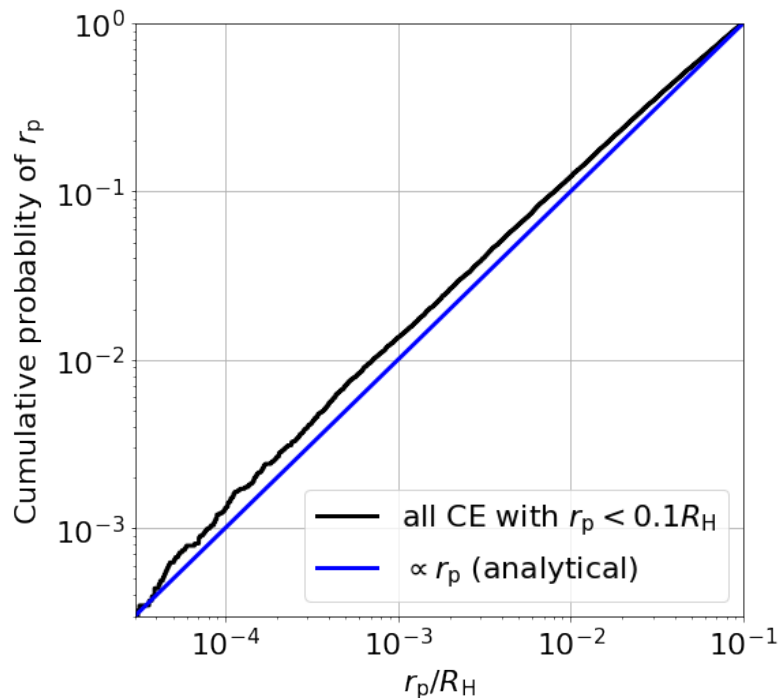


# Reduce CE energy through GW radiation

- $r_p$  needs to be smaller than the critical capture radius:

$$\frac{r_p}{R_H} < \frac{r_{\text{cap}}}{R_H} \simeq 10^{-4}$$

- We show numerically and analytically that  **$r_p$  follows a power-law cumulative probability distribution**, which allows  $r_p$  to be arbitrarily small.



## Calculate the GW capture rate:

Number of binaries formed = (**Probability of  $r_p < r_{\text{cap}}$  for one CE**)  $\times$  (**Number of CEs**)

$$\langle N_{\text{capture}} \rangle \simeq 6 \times 10^{-5} \left( \frac{t}{P_1} \right)^{0.52} \left( \frac{r_{\text{cap}}}{10^{-4} R_H} \right)$$

Fiducial results: Average systems take  $\sim 10^8 P_1$  to get one GW capture.

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*\* We expect these captured binaries to merge quickly. Their mergers will show **high eccentricities** when entering the LIGO band.*

# Dissipation through disk gas

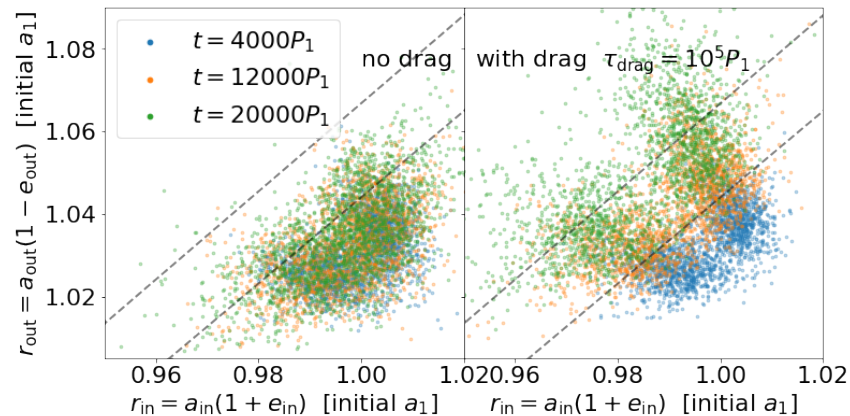
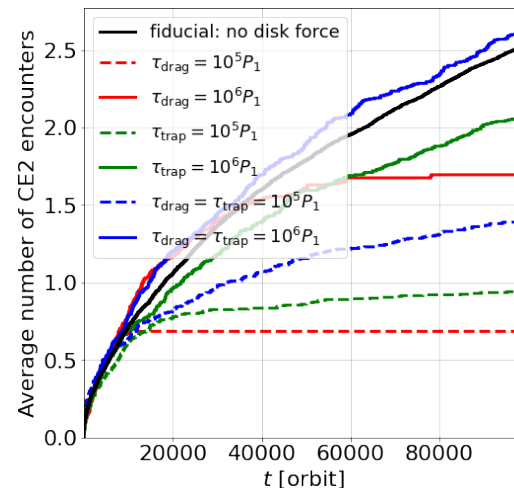
- Drag force and torque from the AGN disk:**

- Considered in our paper:

$$\mathbf{F}_{\text{drag}} = -\frac{\mathbf{v} - \mathbf{v}_K}{\tau_{\text{drag}}},$$

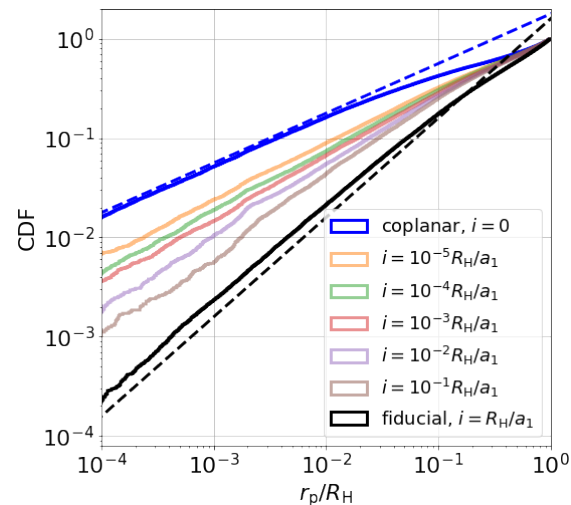
$$\mathbf{F}_{\text{trap}} = -\frac{\Omega_{K,0}(r - r_0)\hat{\theta}}{\tau_{\text{trap}}},$$

- They **do not** increase the GW capture rate.

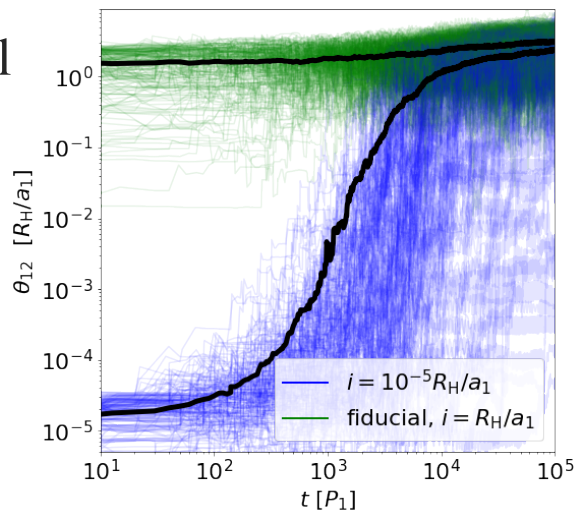


## Inclinations

- Exactly co-planar systems have the highest GW capture rate:  
 $\sim 10^4 P_1$  per capture
- However, exact co-planarity is not realistic because any non-zero small mutual inclination can grow.



Prob( $r_p$ ) changes with the mutual inclination.

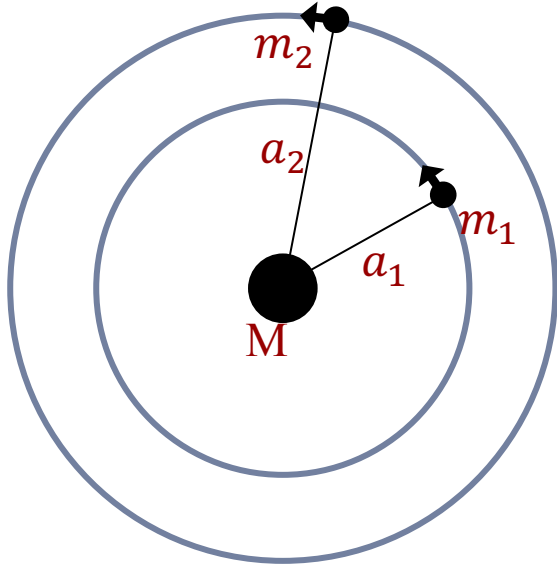


Small mutual inclination converges to our fiducial inclination.

# Takeaways from N-body results

- Dynamical instability in AGN disks produces lots of CEs:
  - Without dissipation, CE pairs are **short-lived**.
  - Separation at CEs can be short enough for GW emission.
- GW radiation can **capture** BHs into binary:
  - With a small probability  $\sim \frac{r_{\text{cap}}}{R_{\text{H}}} \ll 1$ .
  - Number of binaries formed = (Probability of  $r_{\text{p}} < r_{\text{cap}}$  for one CE)  $\times$  (Number of CEs)

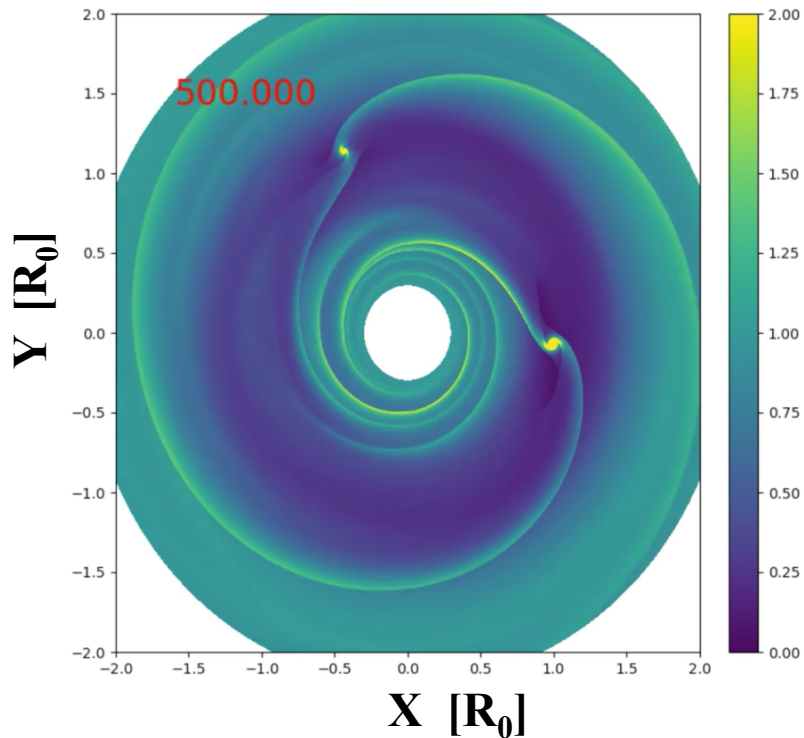
# Formation of BH binaries: hydrodynamics simulations



- Initial condition:

$$a_2 - a_1 = 2R_H$$

# Formation of BH binaries: hydrodynamics simulations

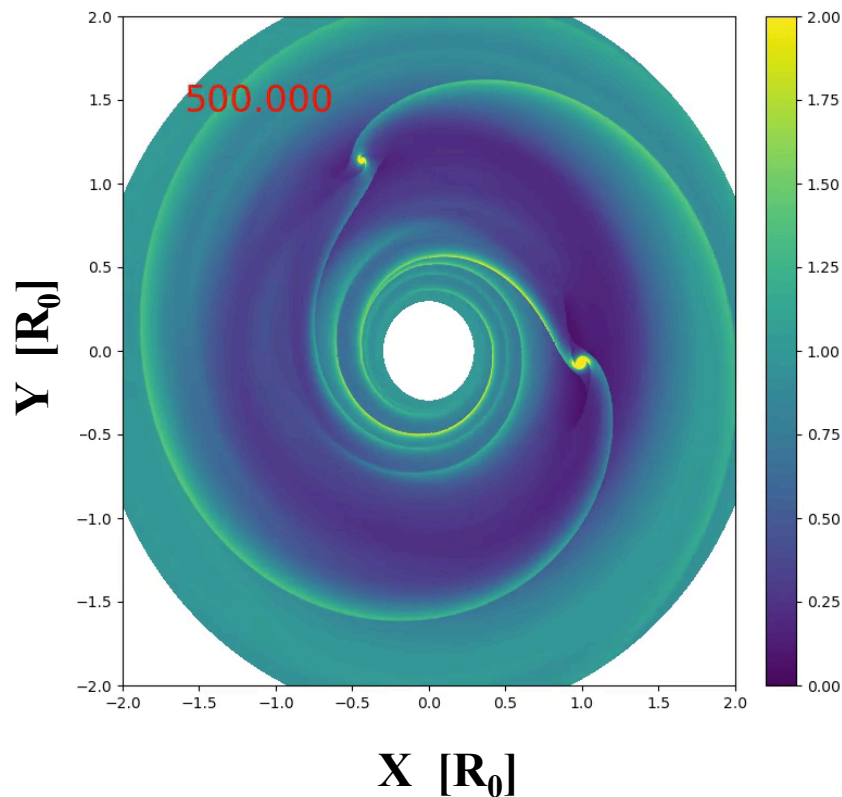


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# Formation of BH binaries: hydrodynamics simulations



(Li+ to be submitted)

- Initial condition:

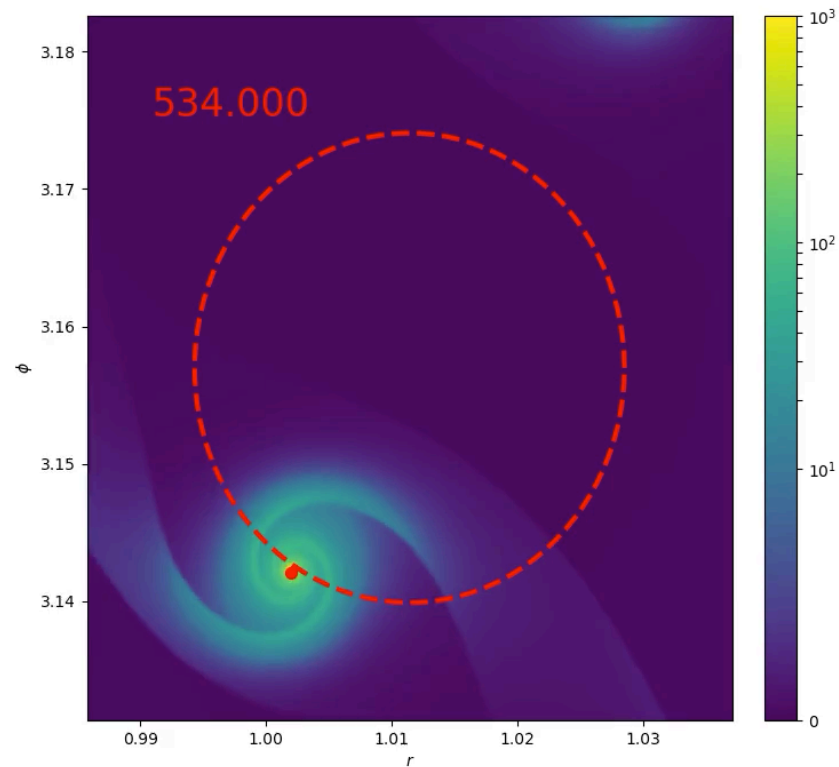
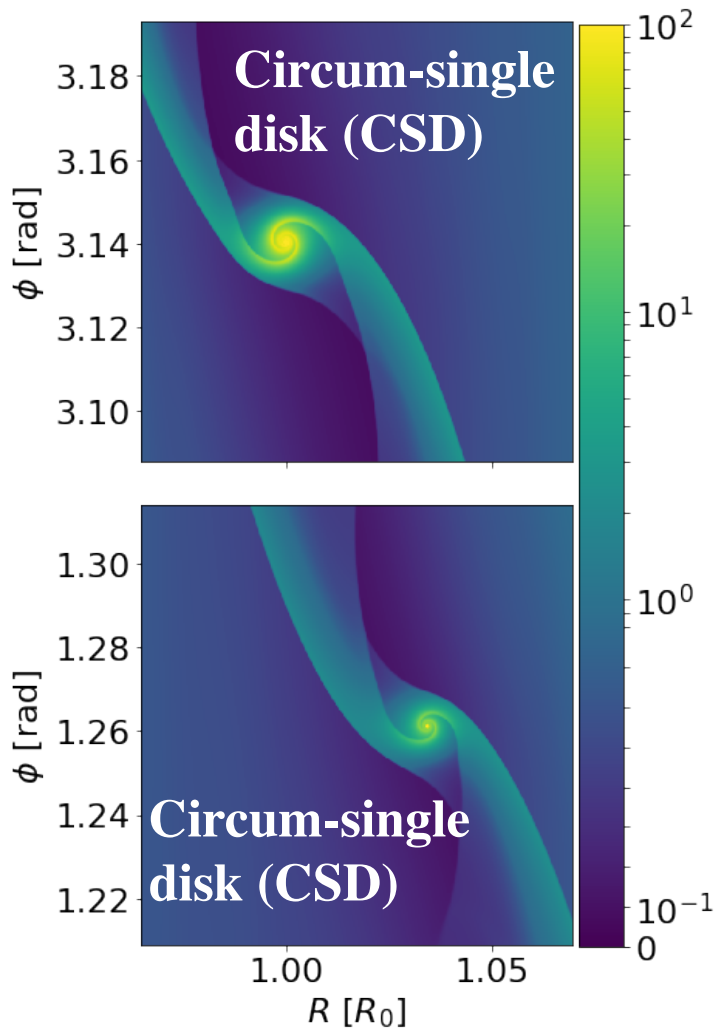
$$a_2 - a_1 = 2R_H$$

(Close encounter at the first conjunction)

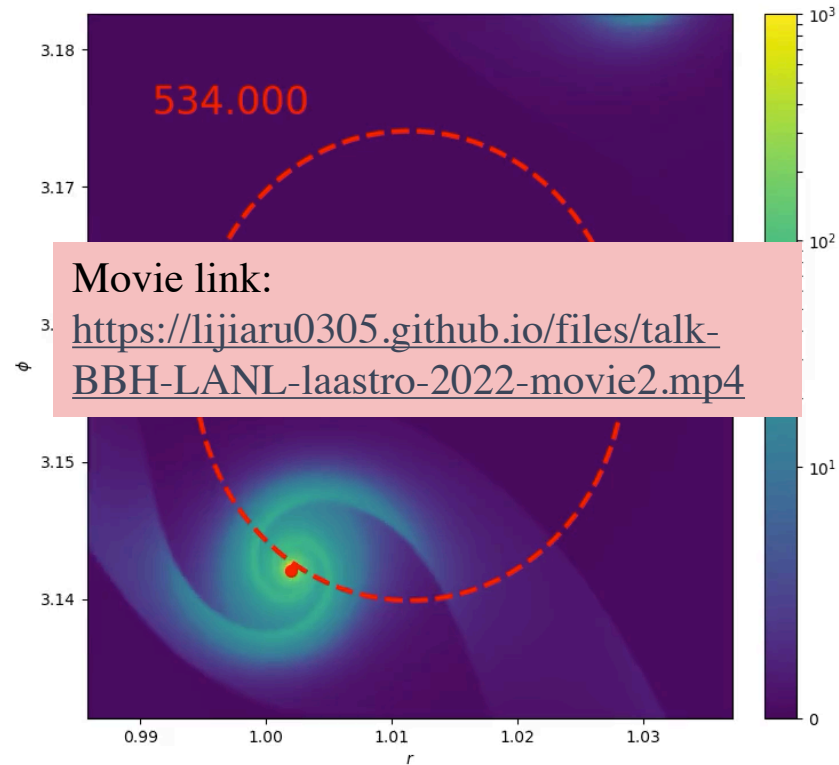
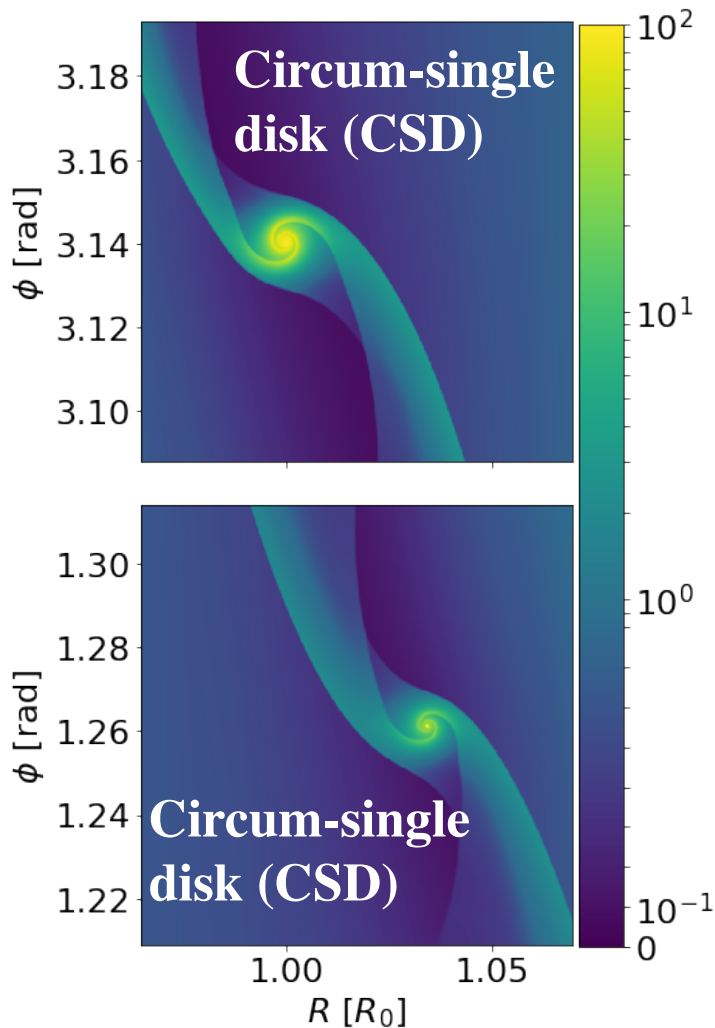
- Simulation setup:

- $M_{\text{SMBH}} = 1$ ,  $m_1 = 10^{-5}$ ,  $m_2 = 5 \times 10^{-6}$
- Thin disk  $H/R = 0.01$ , low viscosity  $\alpha = 0.01$ .
- Isothermal disk.
- High resolution with  $50 \rightarrow 100$  grid cells per  $R_H$ , where  $R_H = 0.017R_0$

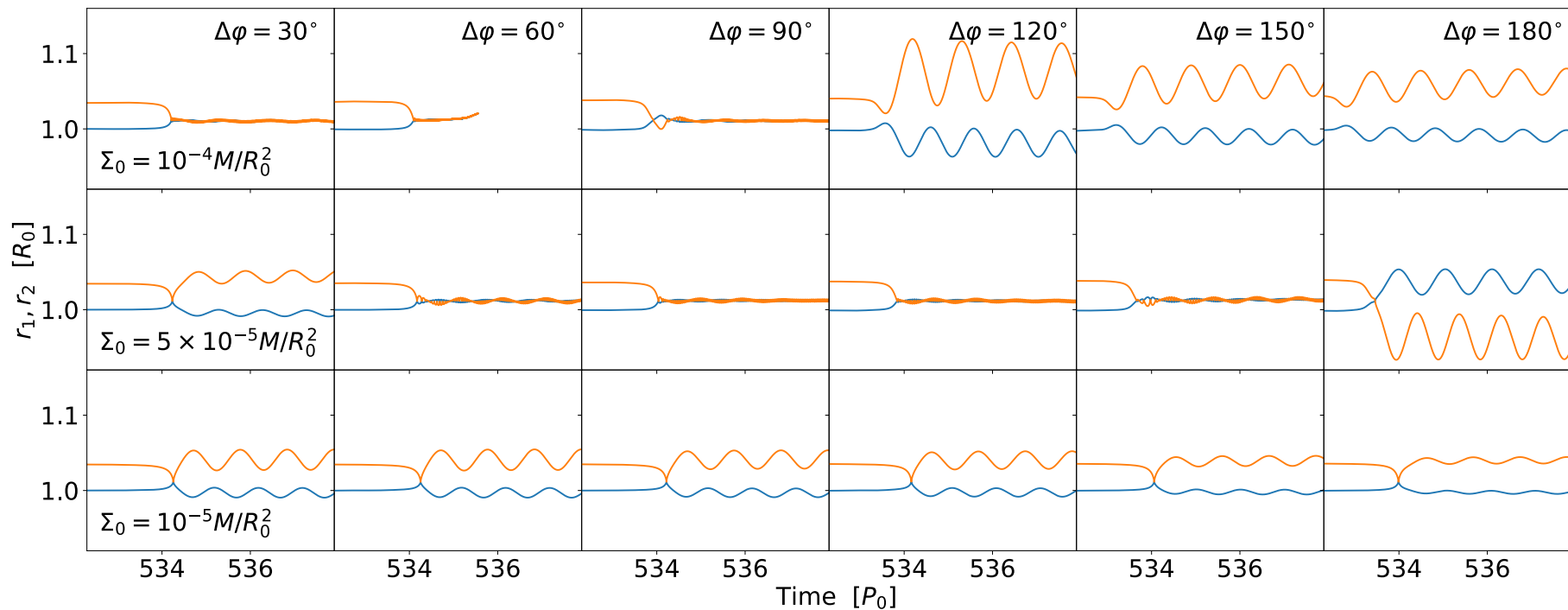
## Formation of a binary



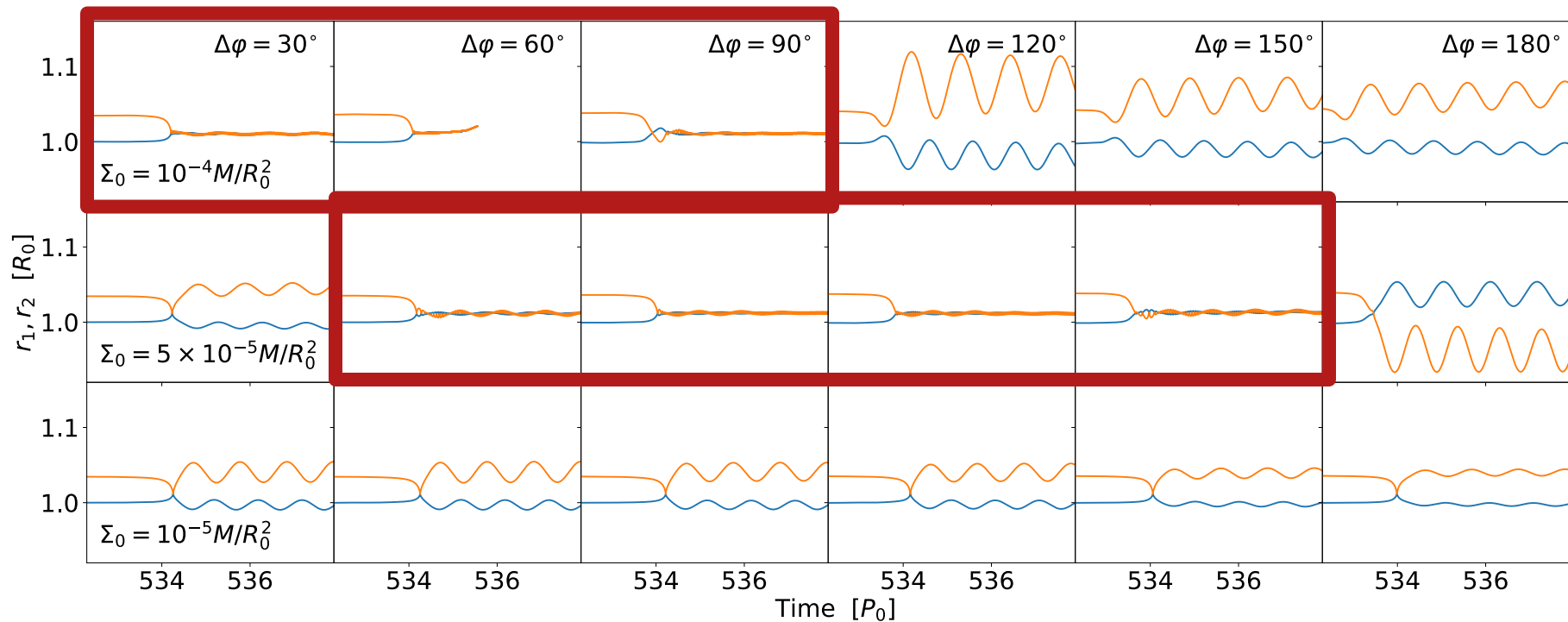
# Formation of a binary



# Simulation outcomes

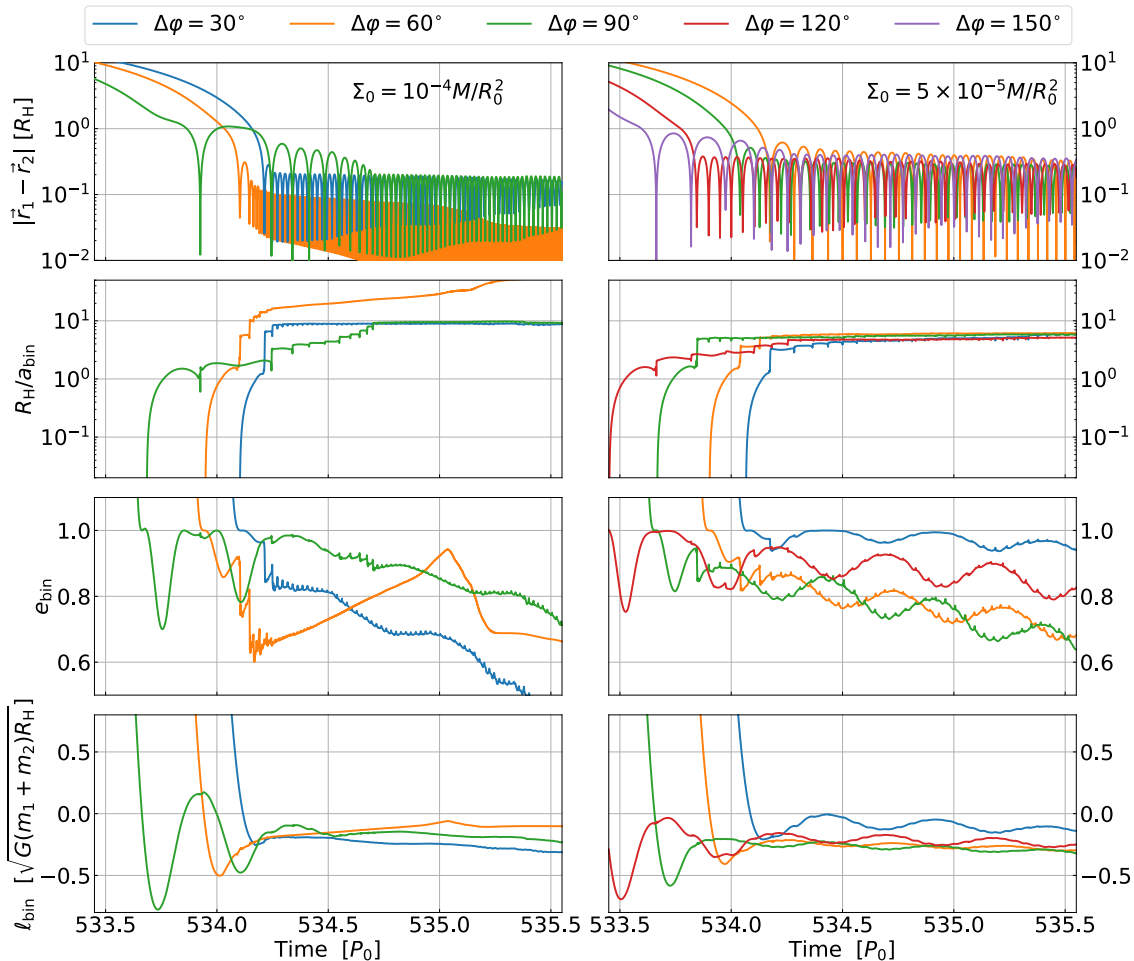


# Simulation outcomes

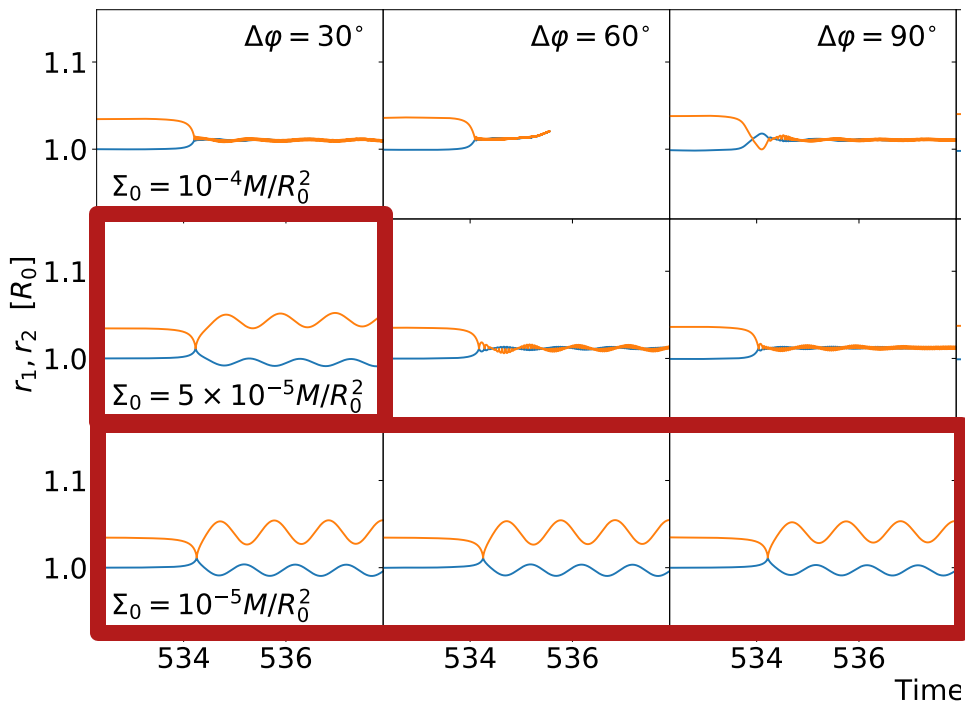


# Resulting binary orbit after formation

- small semi-major axis:  $\frac{a_{\text{bin}}}{R_{\text{H}}} \sim 0.1$
- large eccentricity:  $e_{\text{bin}} > 0.5$
- retrograde rotation:  $\ell_{\text{bin}} < 0$



## (for those are interested..) No-formation cases...

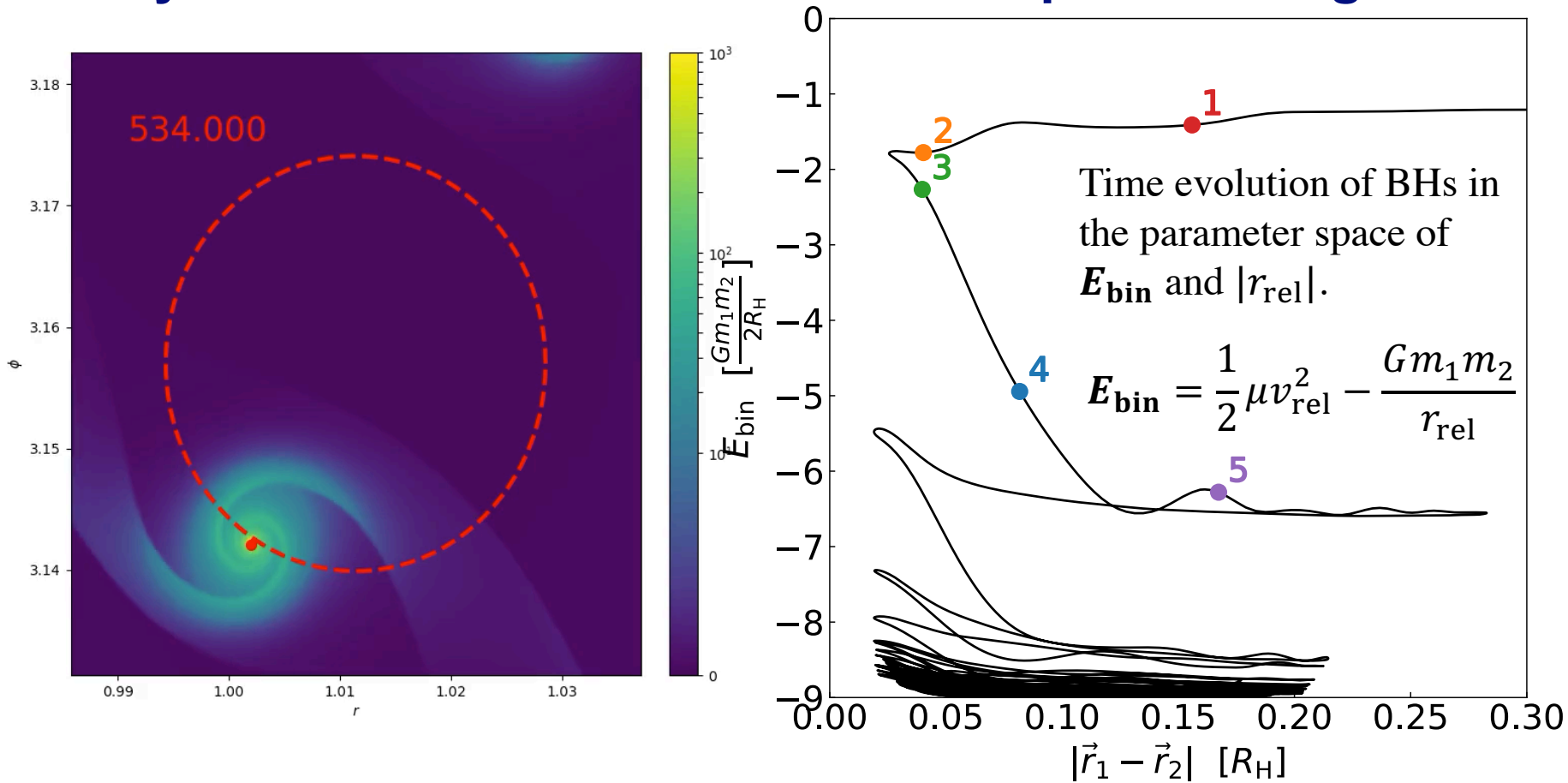


We focus on the outcome of the first close encounters.

But, just to point out the following considerations:

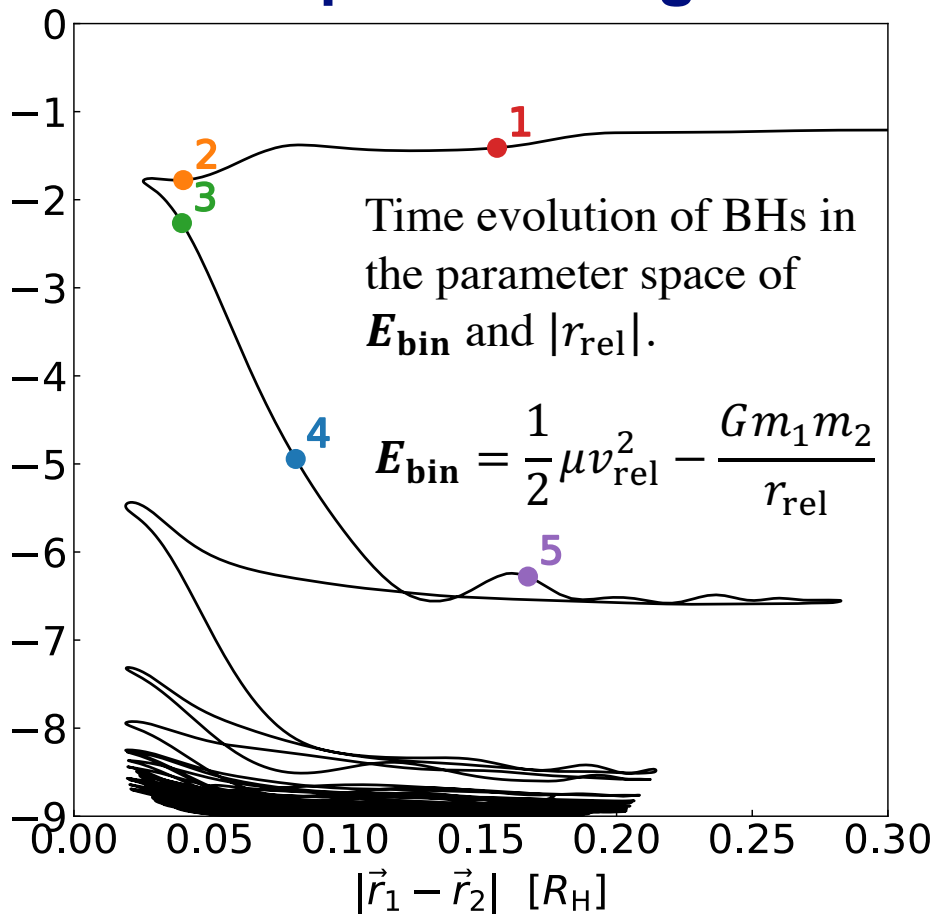
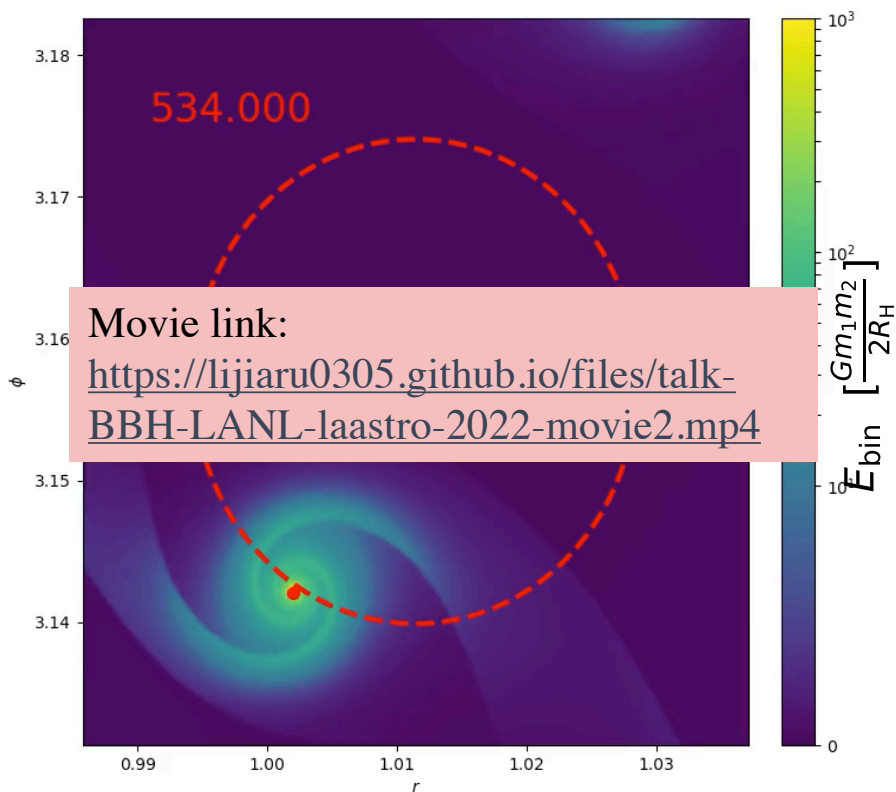
- eccentricity damping
- orbital migration
- ...

# Analysis: formation mechanism -- a departure drag

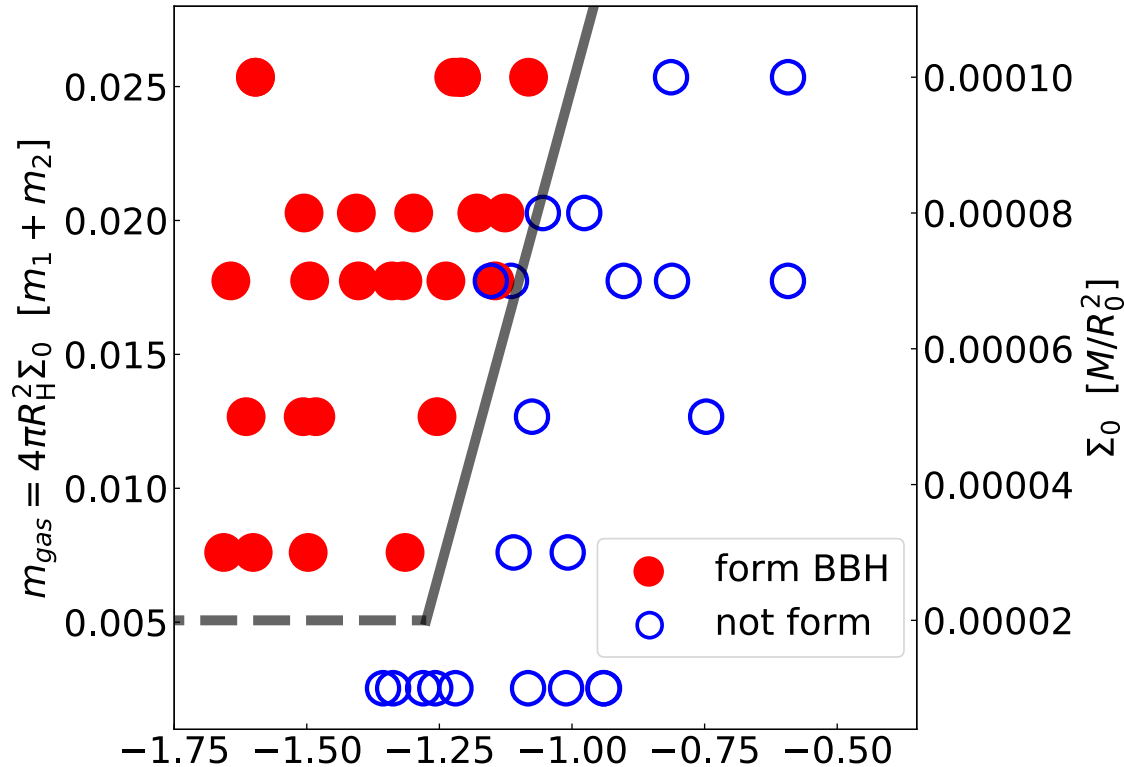




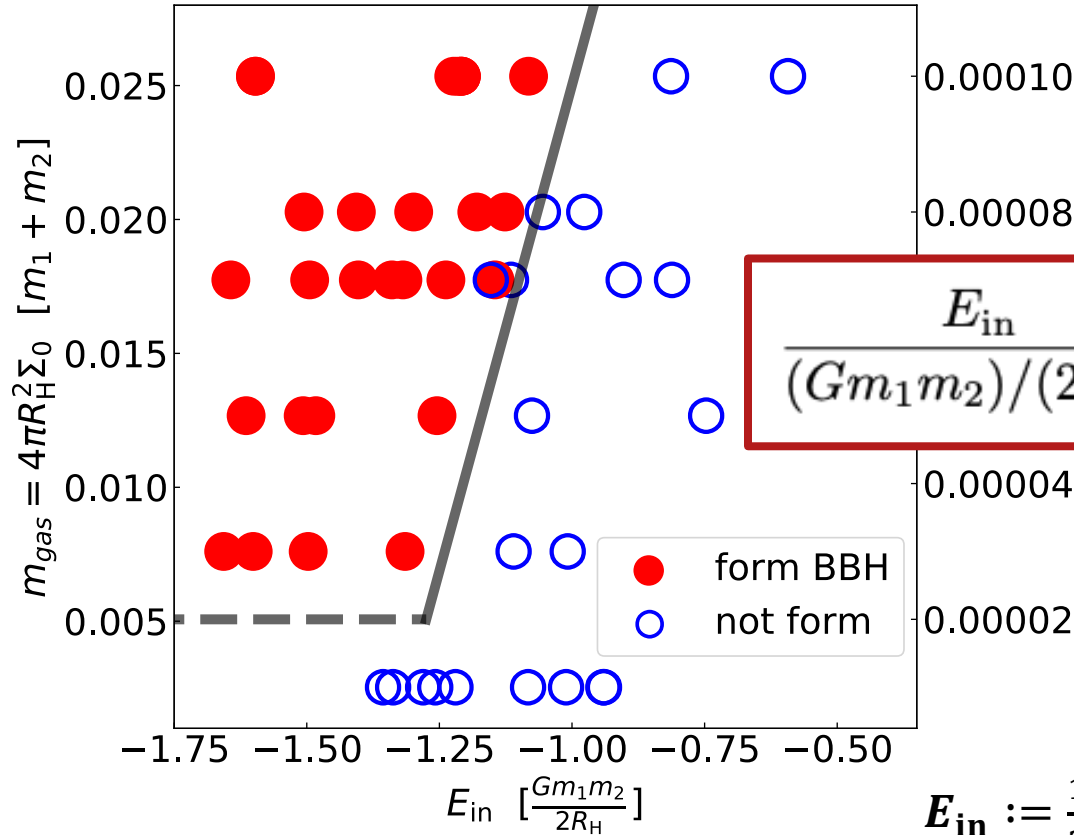
# Analysis: formation mechanism -- a departure drag



# Analysis: criteria for binary formation



# Analysis: criteria for binary formation



$$\frac{E_{\text{in}}}{(Gm_1 m_2)/(2R_{\text{H}})} < 13.78 \frac{m_{\text{gas}}}{(m_1 + m_2)} - 1.344$$

$$E_{\text{in}} := \frac{1}{2} \mu v_{\text{rel}}^2 - \frac{Gm_1 m_2}{r_{\text{rel}}} \text{ when } r_{\text{rel}} = 0.3R_{\text{H}}$$

# Summary

- Mergers of BH binaries embedded in AGN disks are considered important sources of gravitational wave.
- When the gas effect is negligible, dynamical instability produces lots of close encounters. → In rare events of every deep encounters, with a certain probability, very tightly-bounded captured binaries can form.
- When the gas density is sufficiently high, close encounters can form bound binaries due to the collision between the two CSDs. → Increases the formation-per-encounter ratio.
- The resulting BH binary orbits can be highly eccentric, compact, and retrograde. → May be considered as the “initial configuration” of the “pre-existing” binaries.